

Week 2: Wednesday

EECS 281

Agenda

Templates

Standard Template Library

Containers

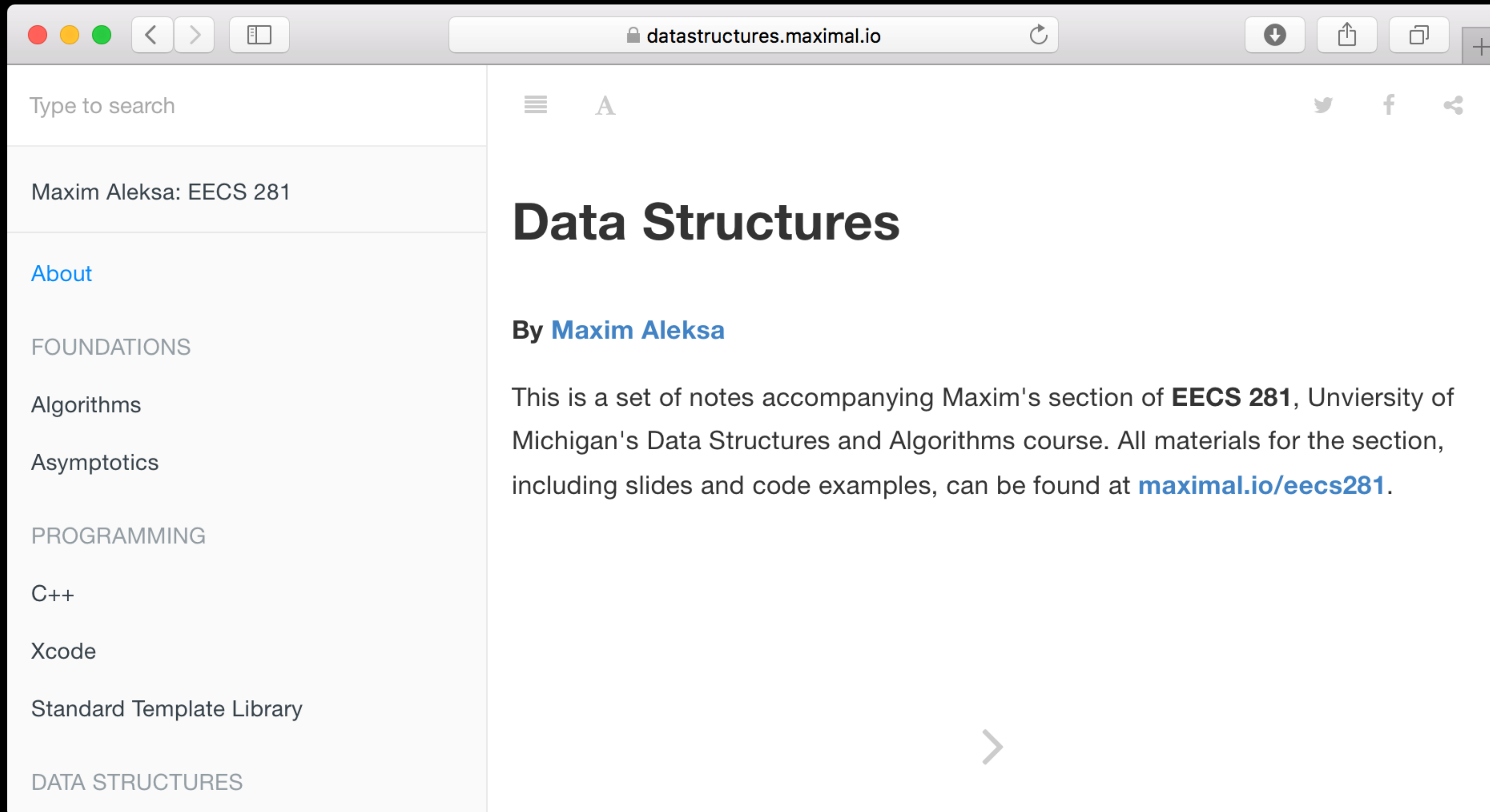
Array

Vector

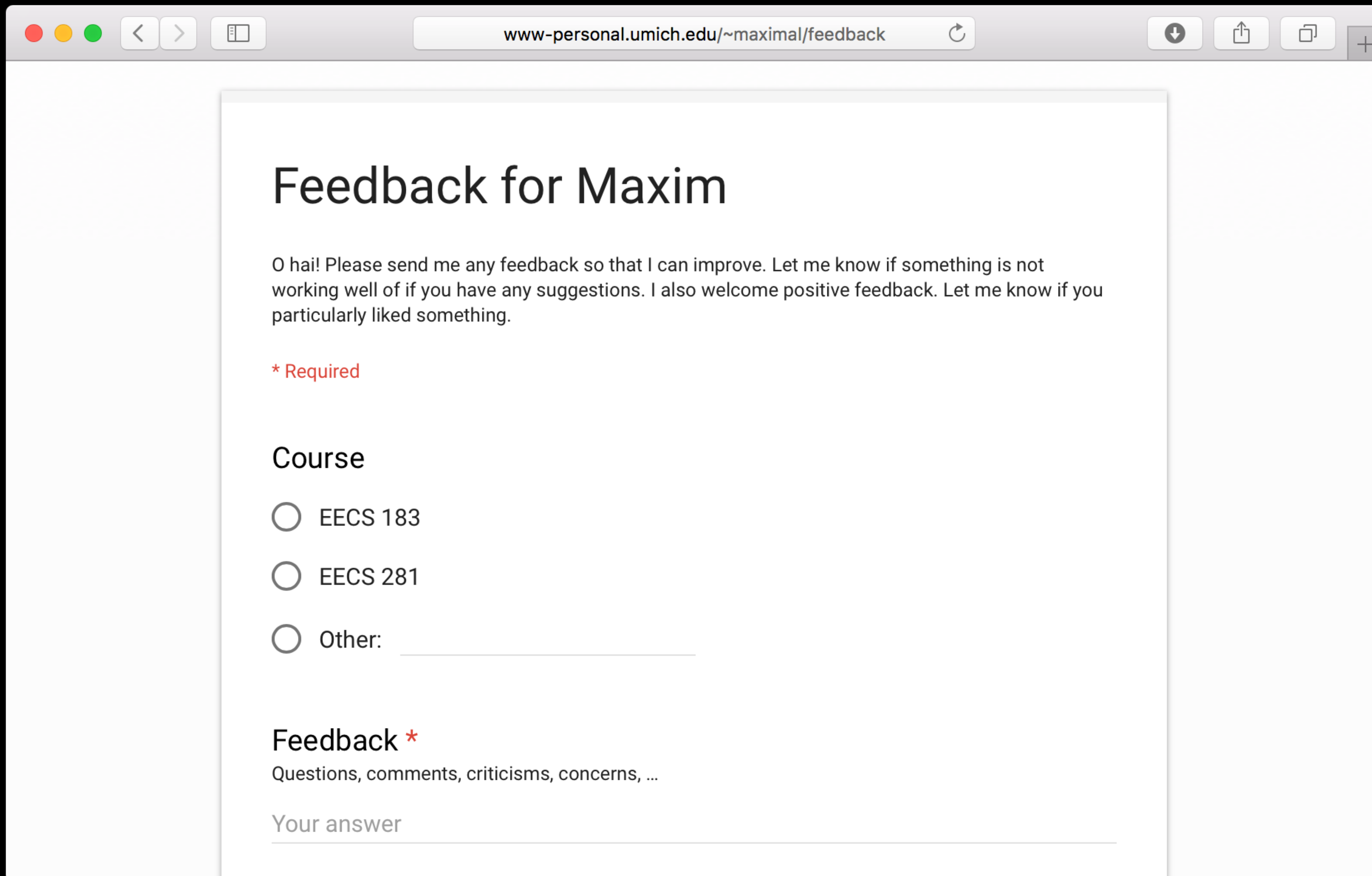
Deque

(Linked) list

datastructures.maximal.io



maximal.io/feedback



The screenshot shows a web browser window with the address bar displaying `www-personal.umich.edu/~maximal/feedback`. The page content is a feedback form titled "Feedback for Maxim". The form includes a welcome message, a required field for "Course" with radio button options for "EECS 183", "EECS 281", and "Other:", and a required text field for "Feedback".

Feedback for Maxim

O hai! Please send me any feedback so that I can improve. Let me know if something is not working well of if you have any suggestions. I also welcome positive feedback. Let me know if you particularly liked something.

* Required

Course

☐ EECS 183

☐ EECS 281

☐ Other: _____

Feedback *

Questions, comments, criticisms, concerns, ...

Your answer _____

Sorting

Improving complexity

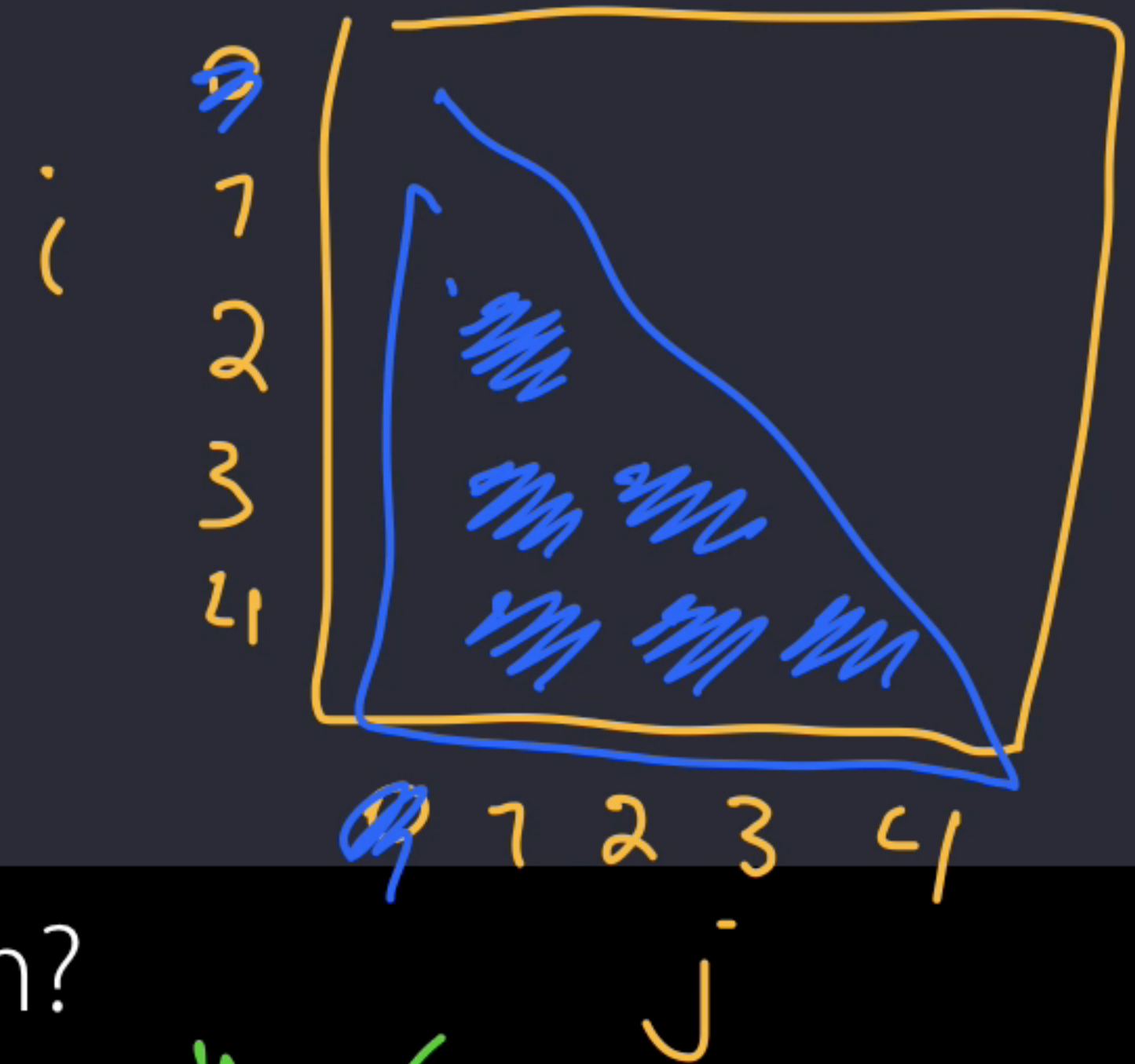
Sorting

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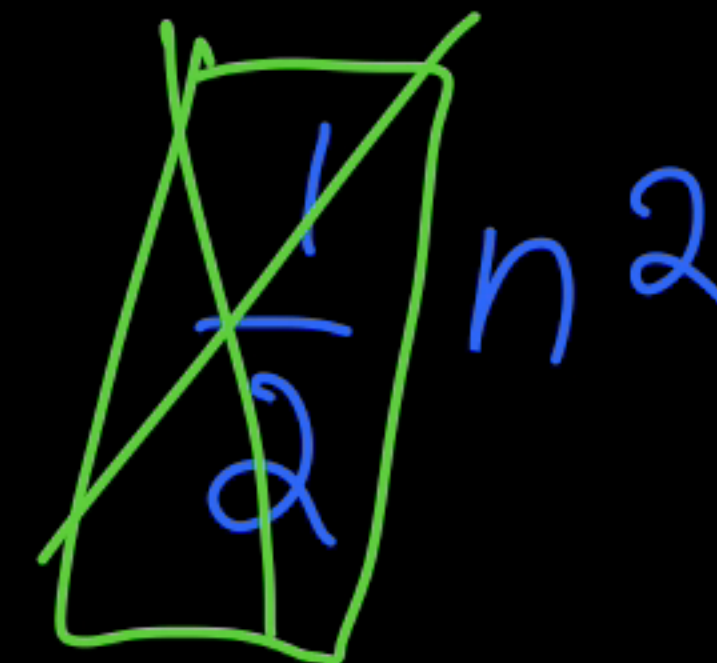
What is the growth complexity of this algorithm?

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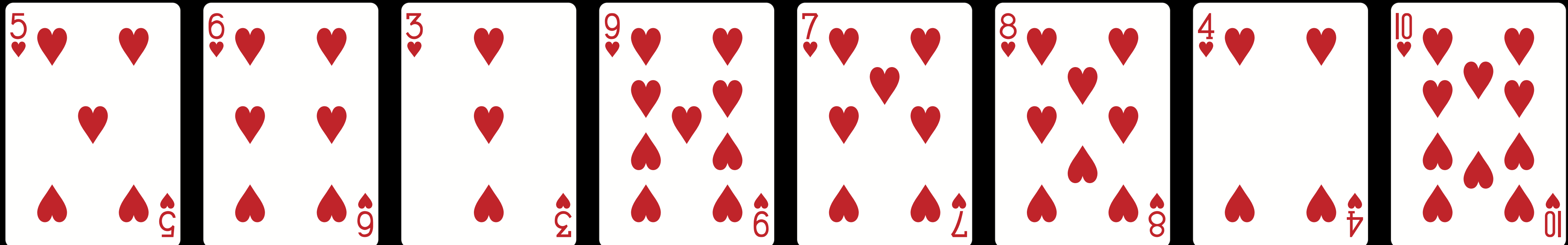
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unsorted

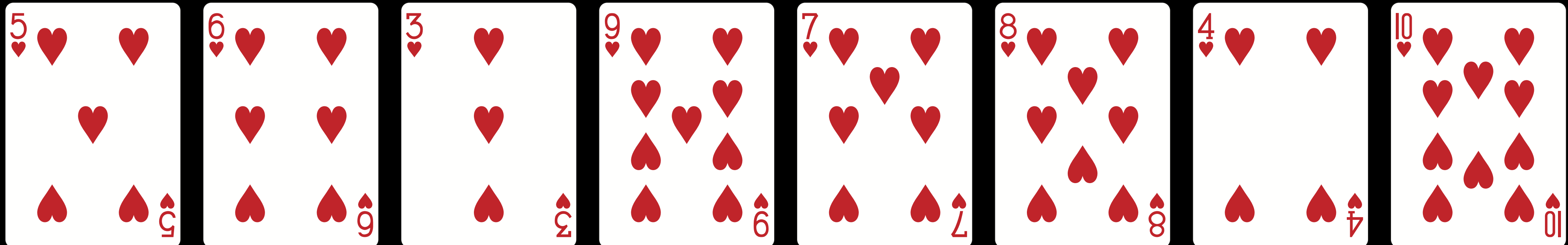


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sorted

unsorted

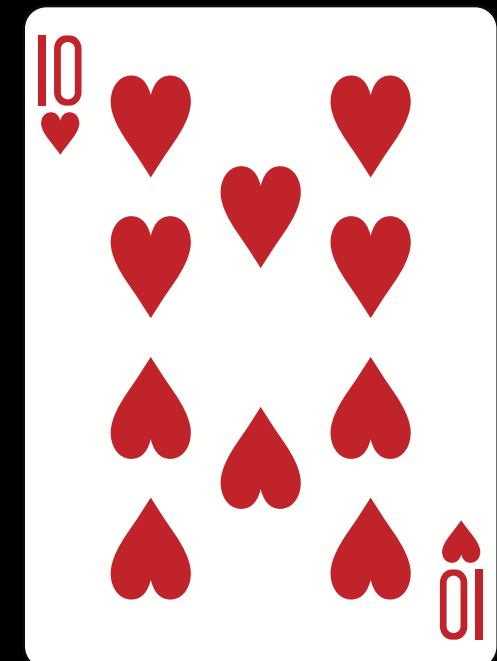
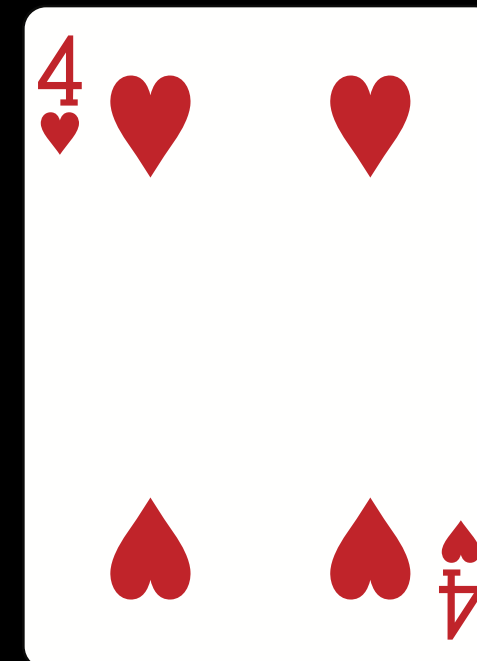
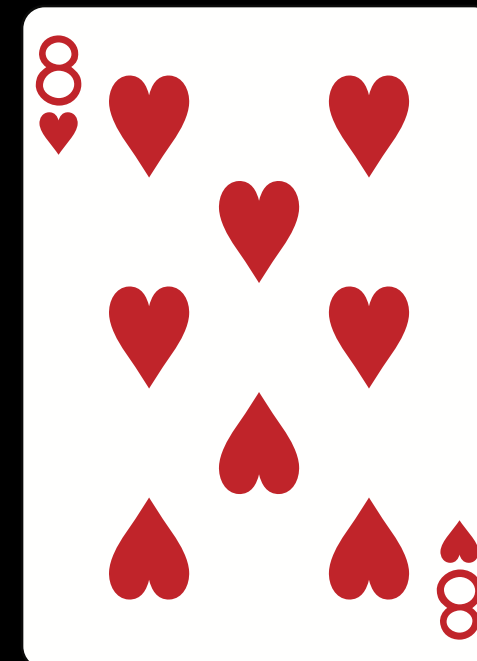
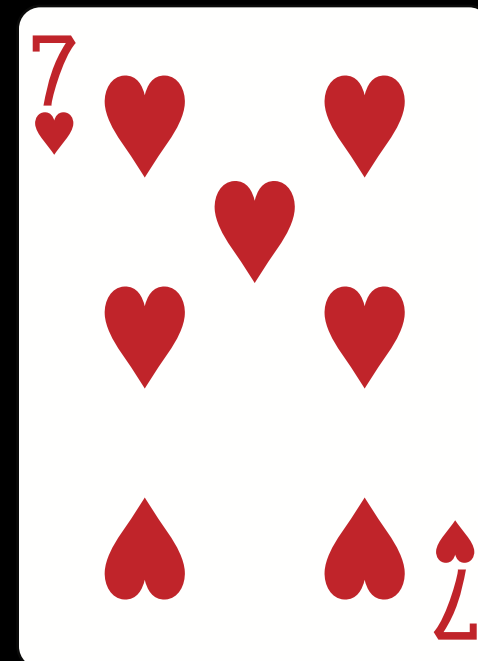
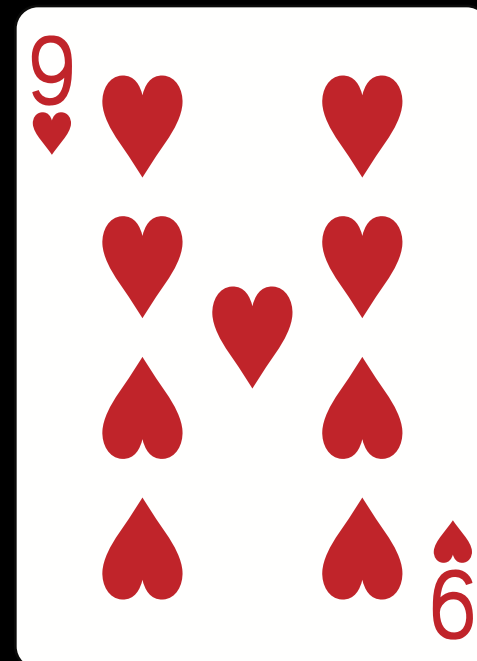
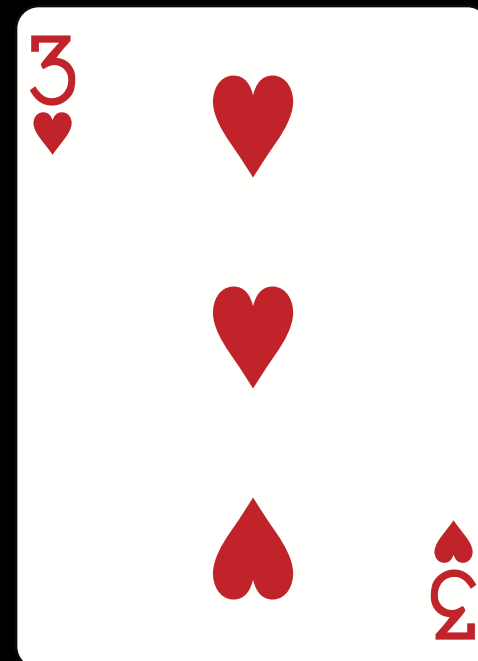
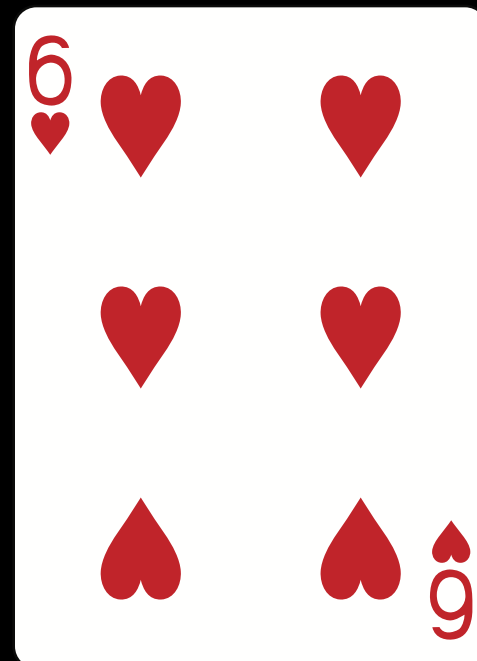
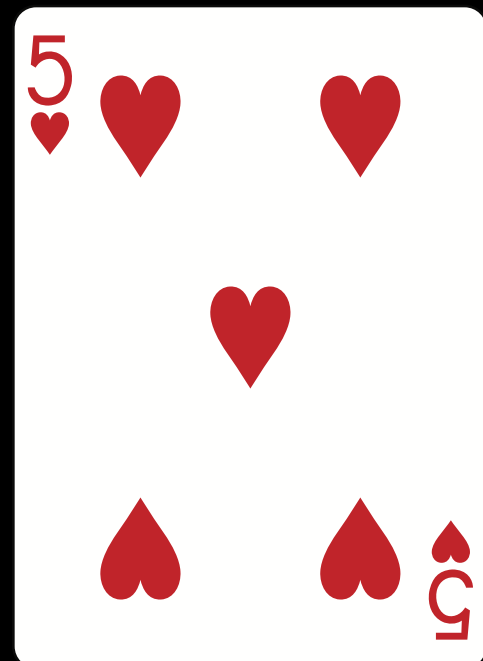


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sorted

unsorted

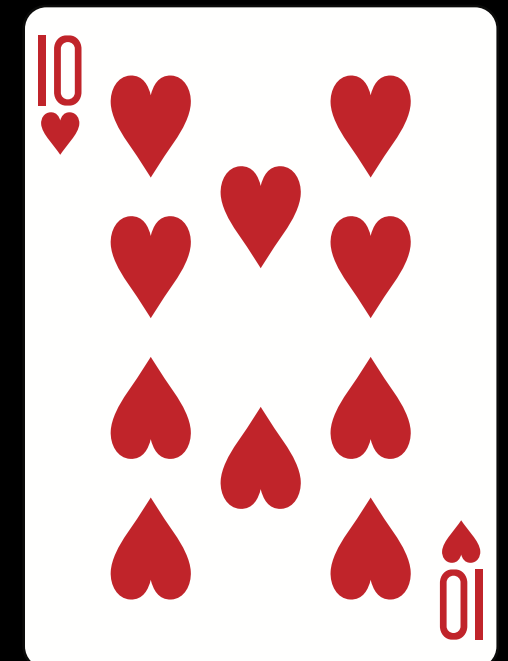
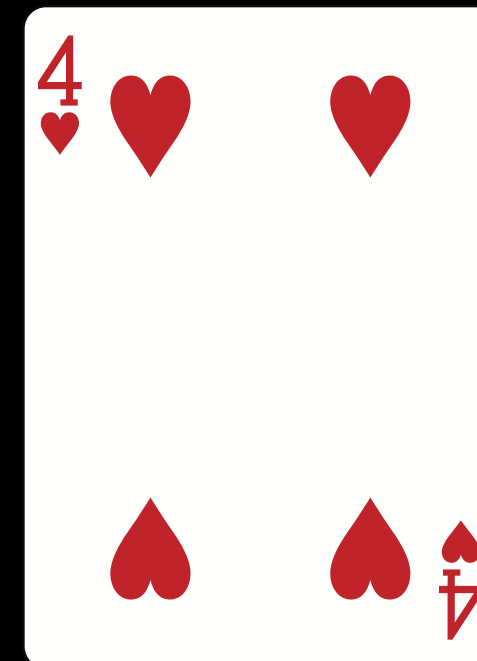
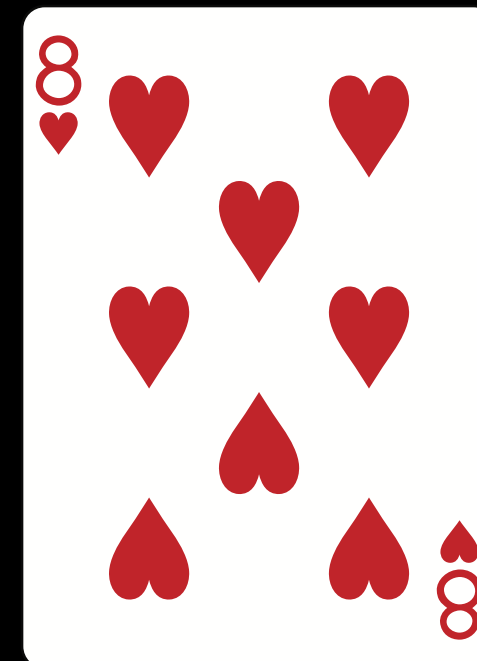
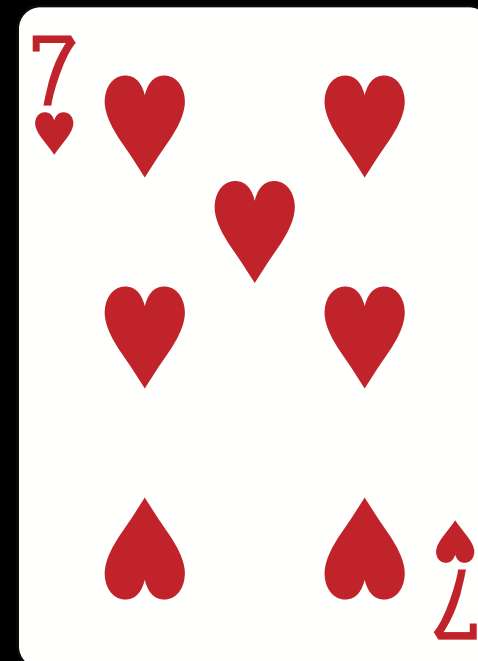
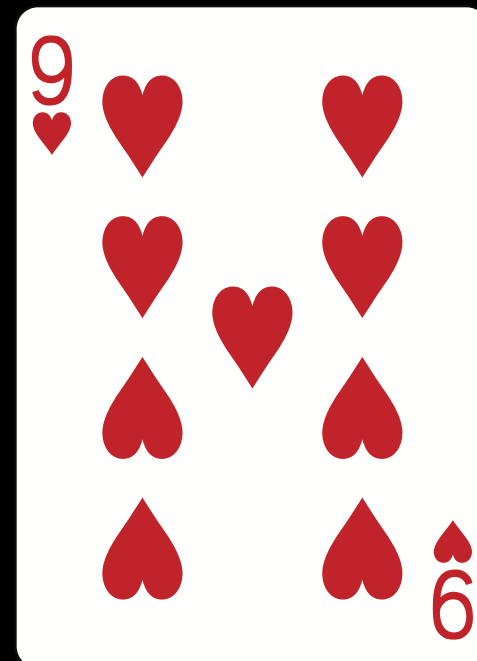
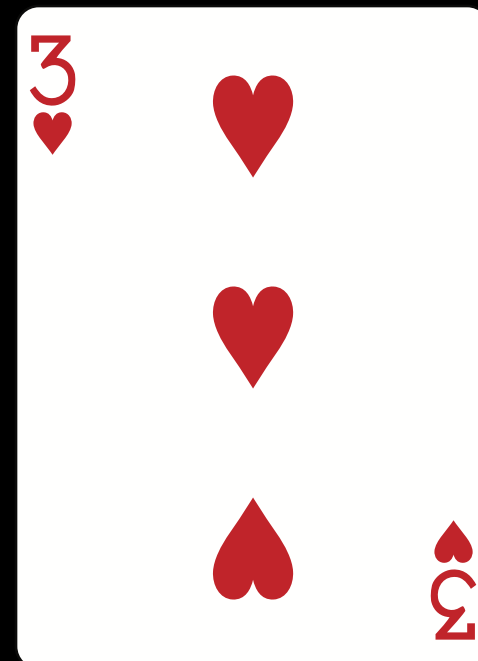
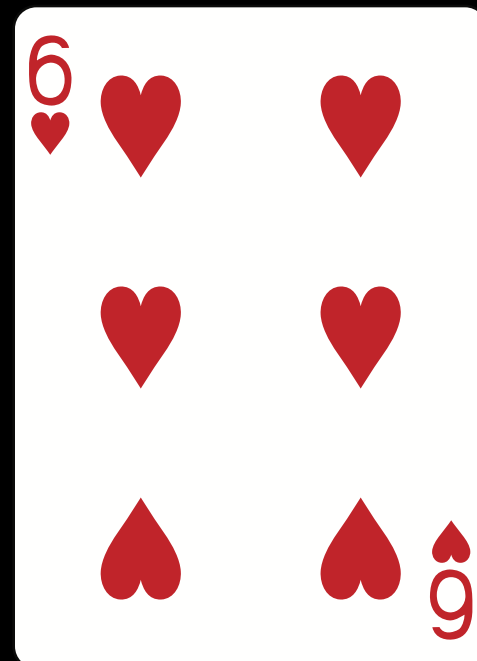
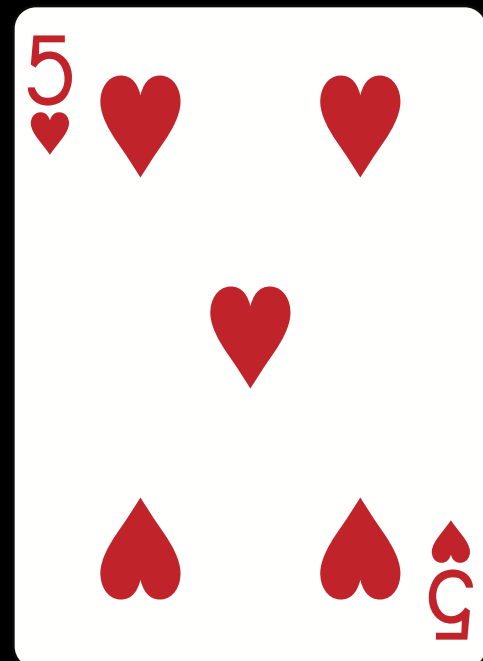


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sorted

unsorted

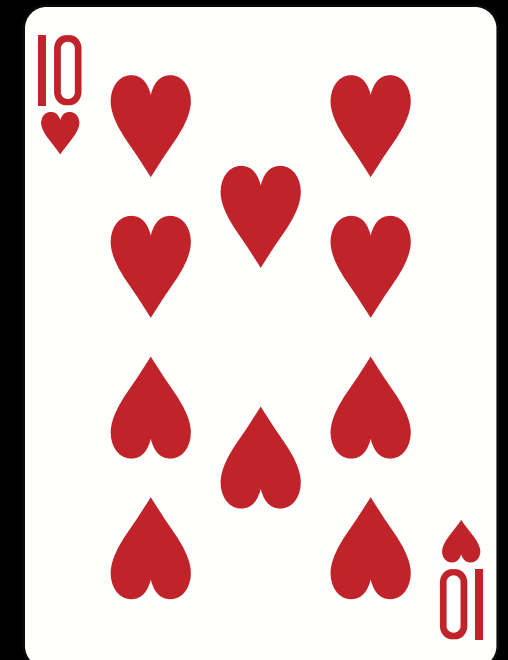
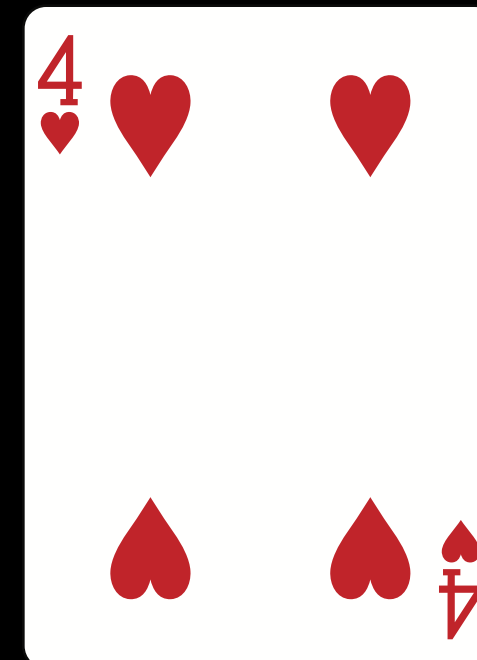
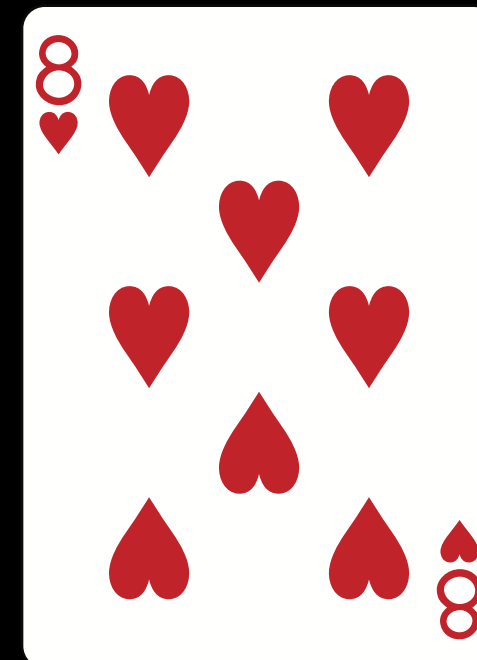
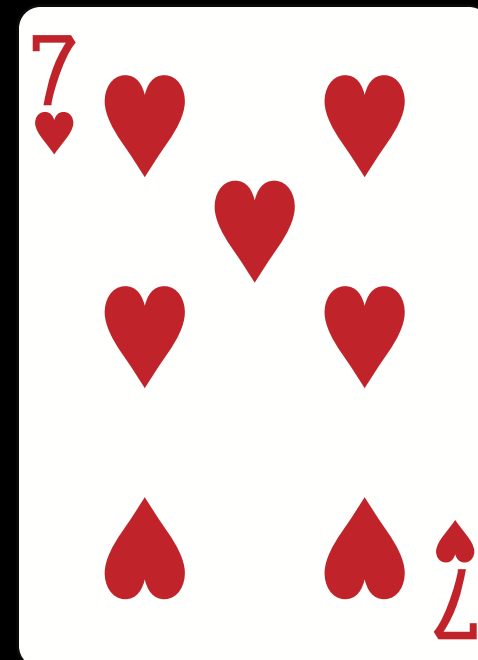
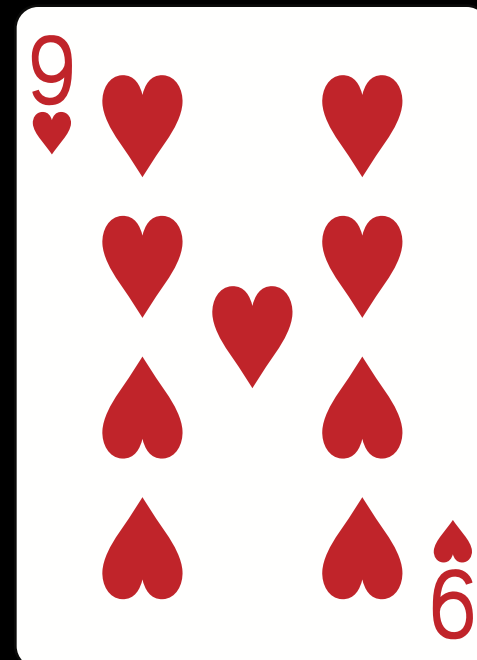
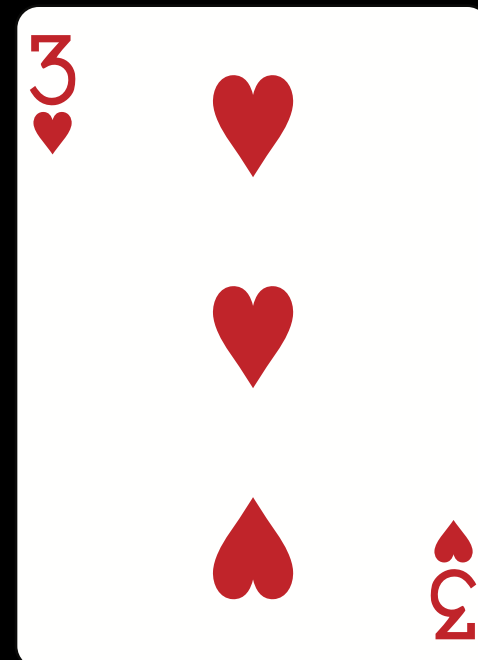
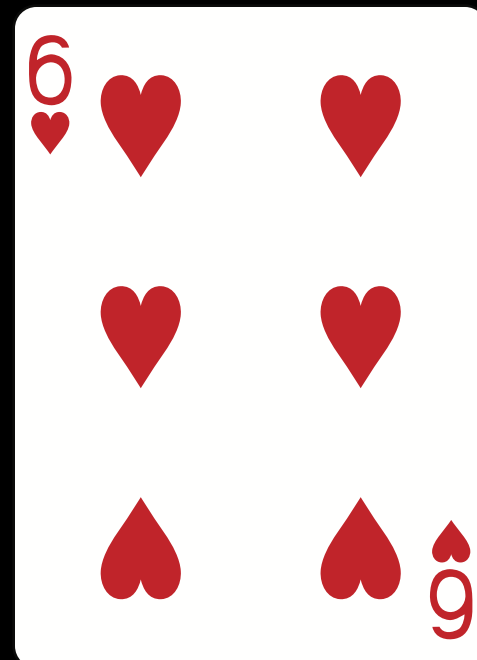
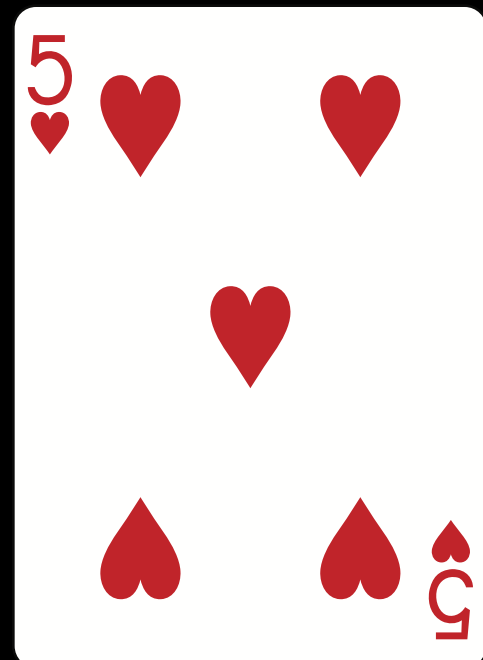


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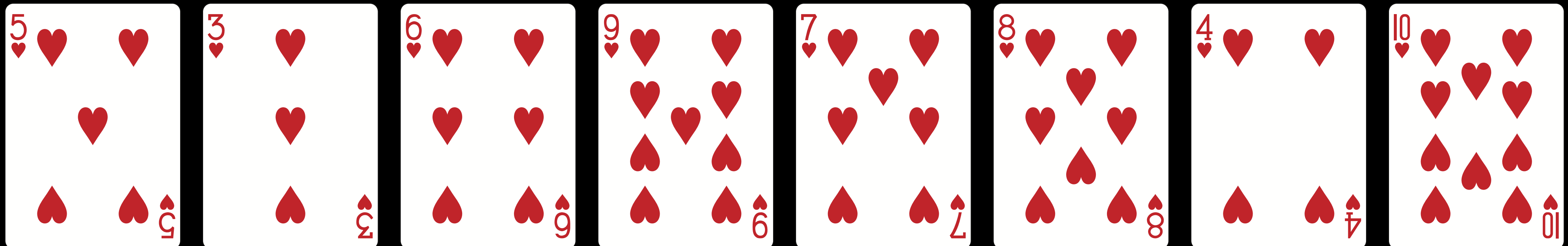
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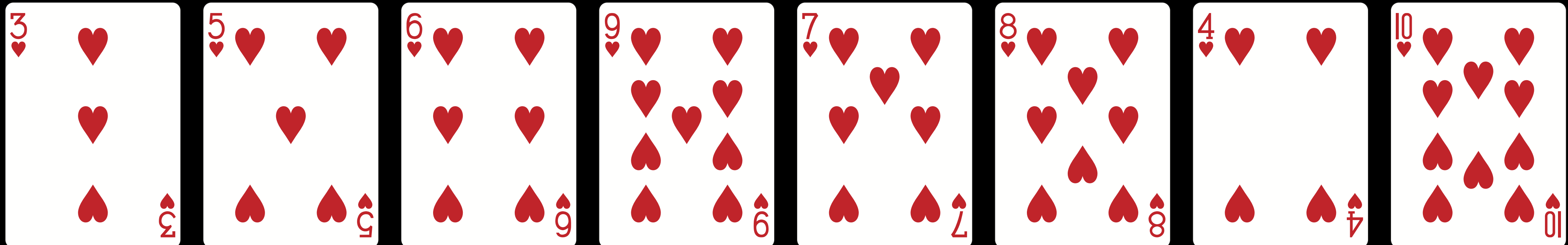


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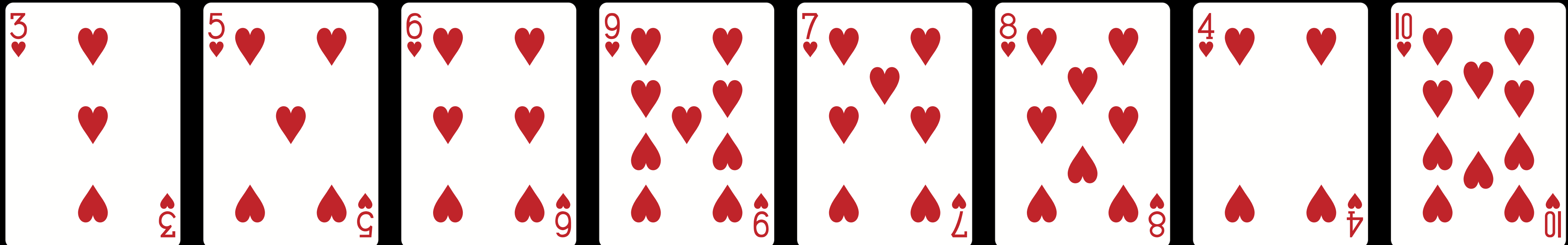


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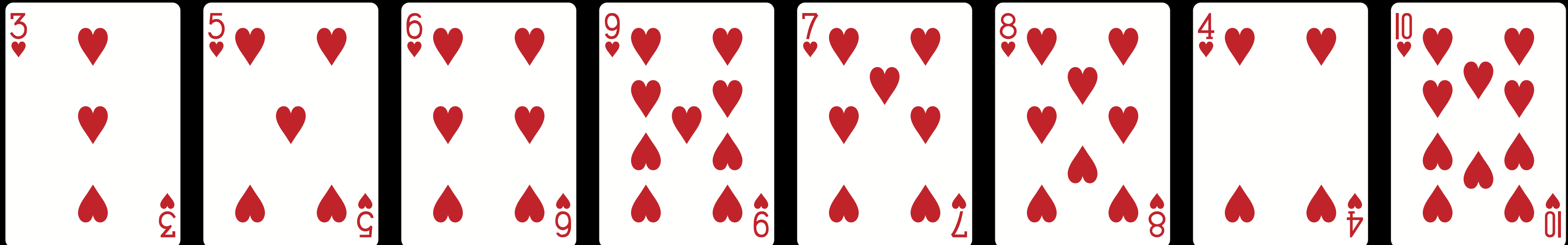


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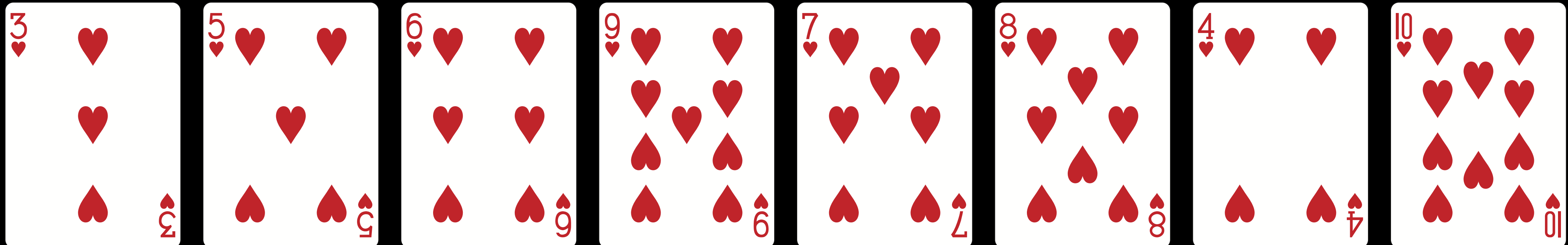


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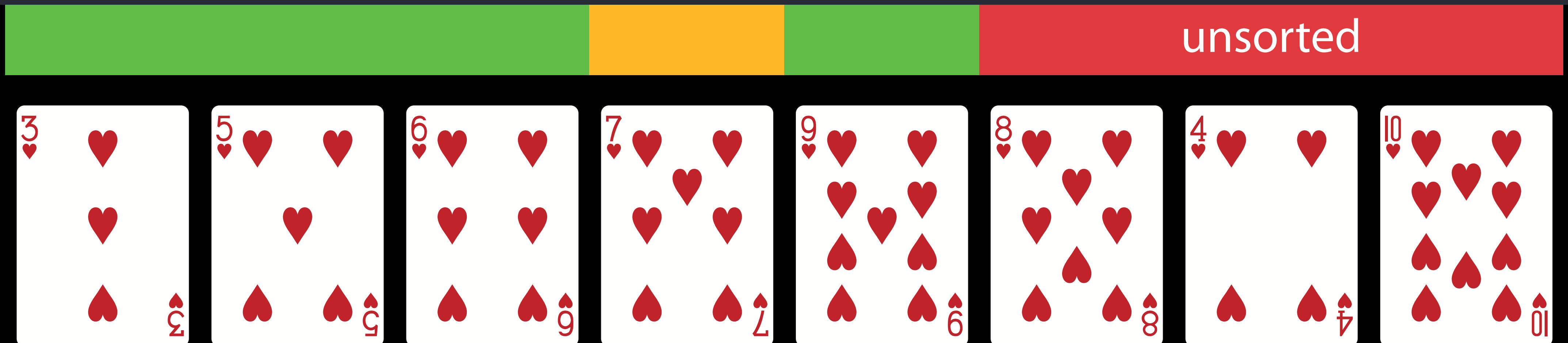
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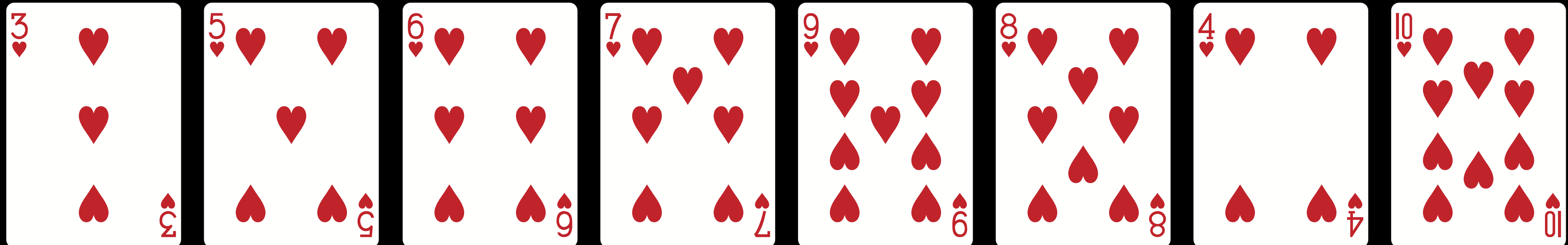


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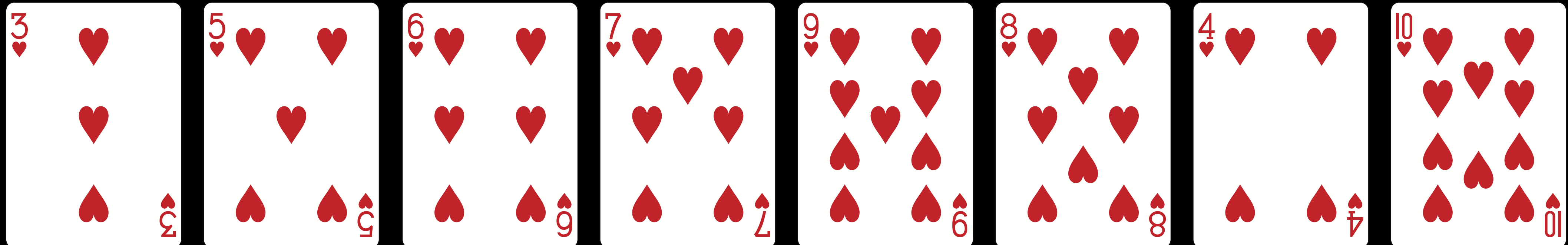


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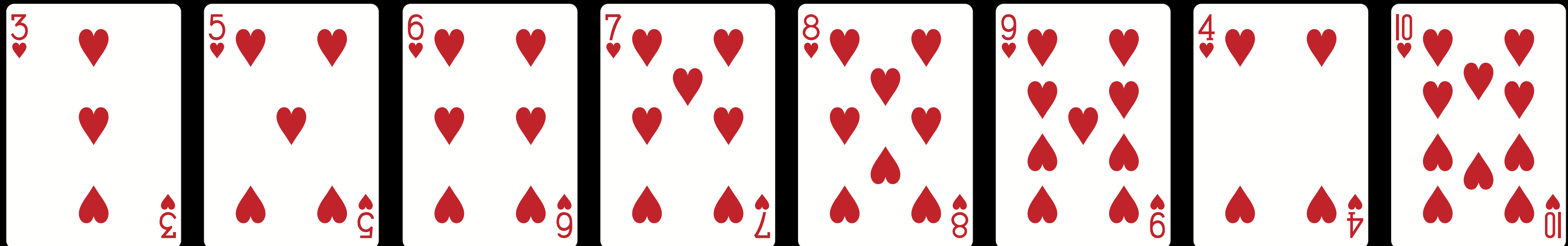
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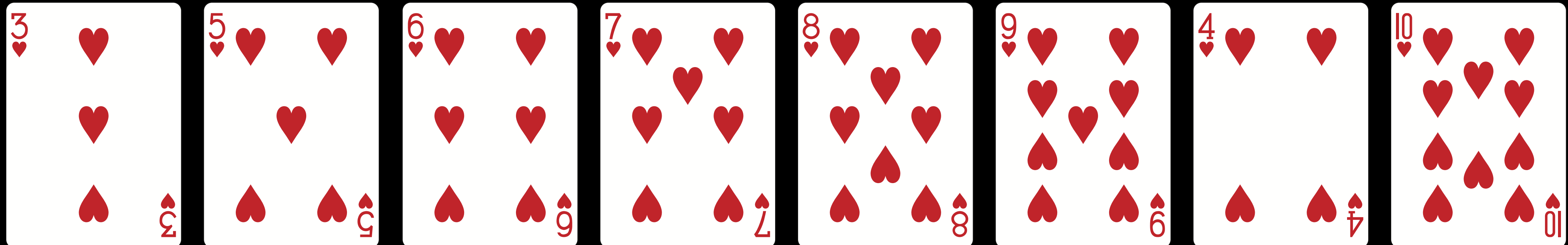


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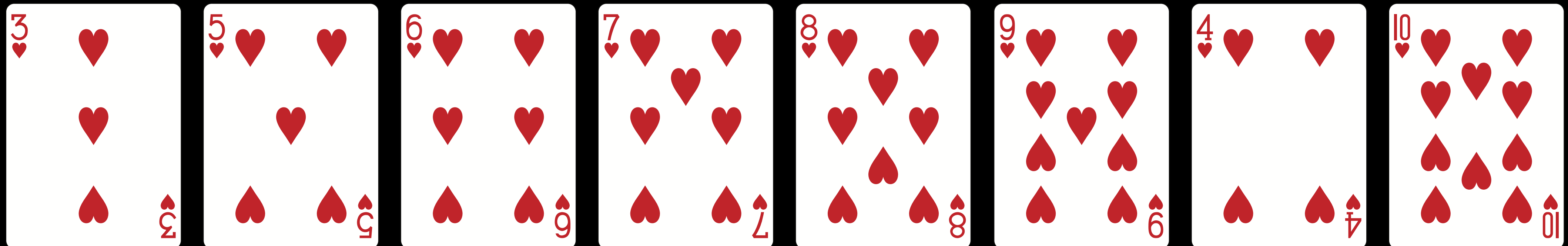


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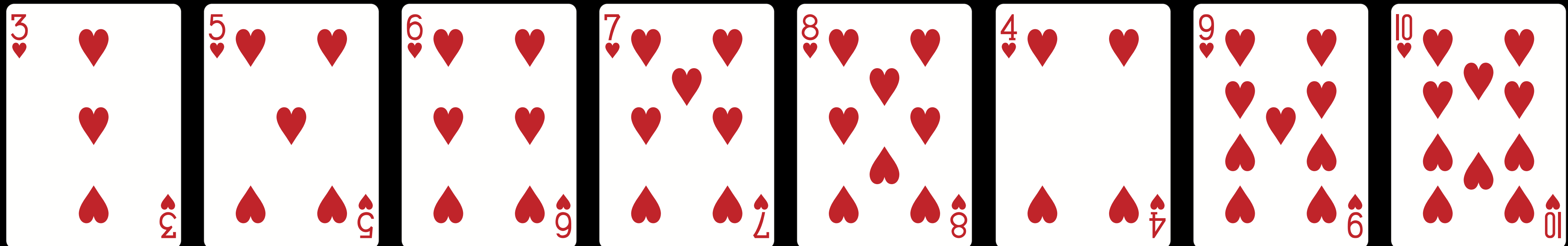
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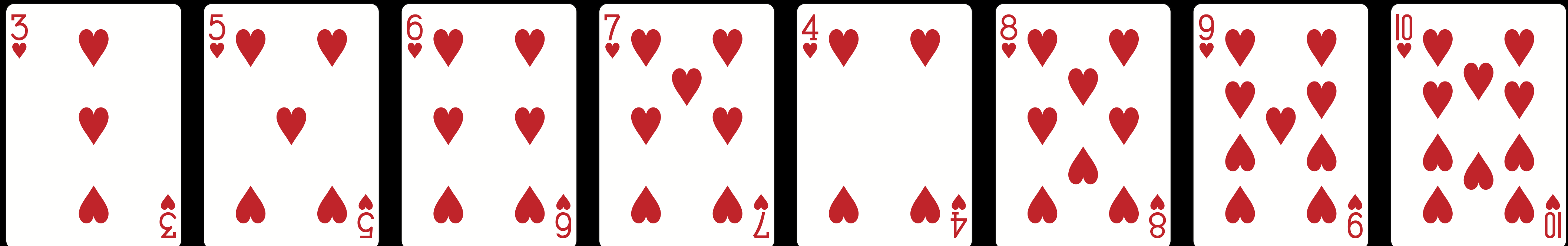
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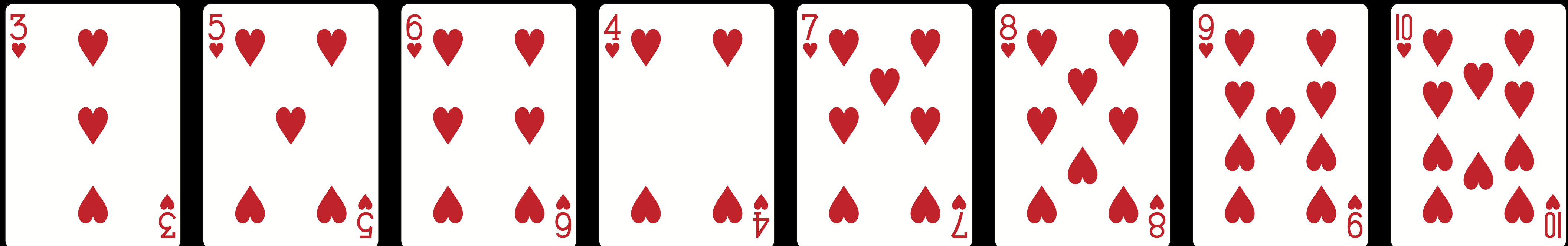
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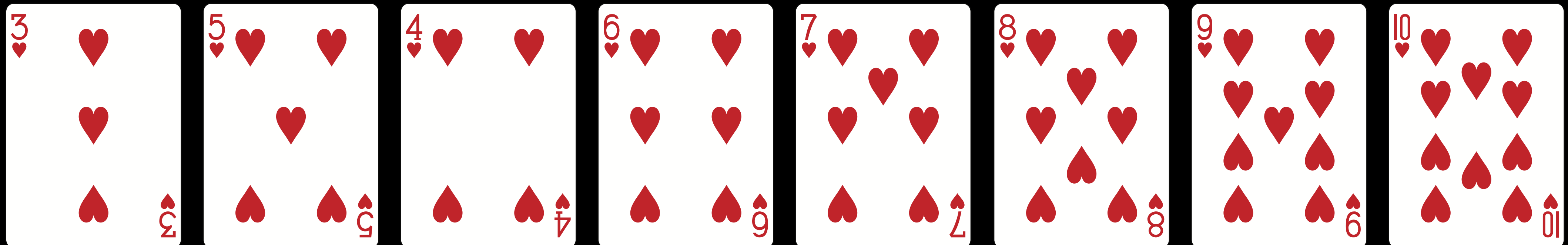
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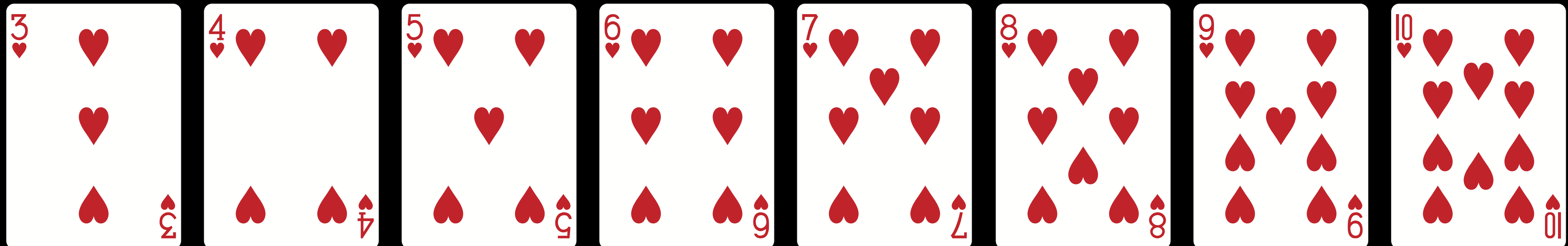
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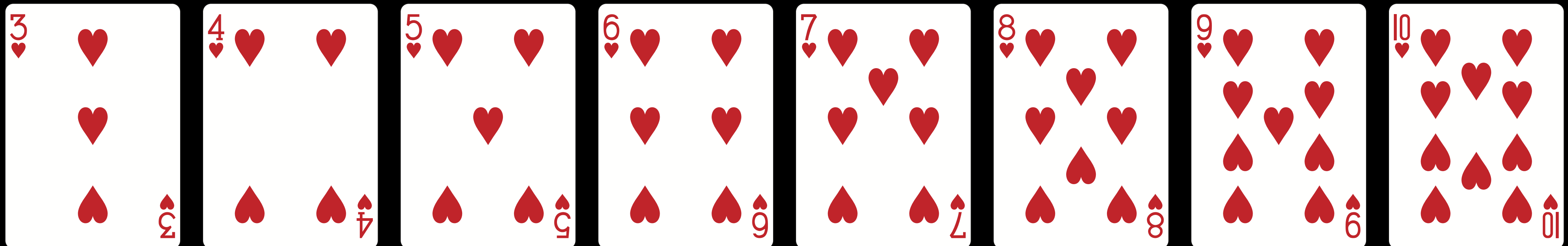


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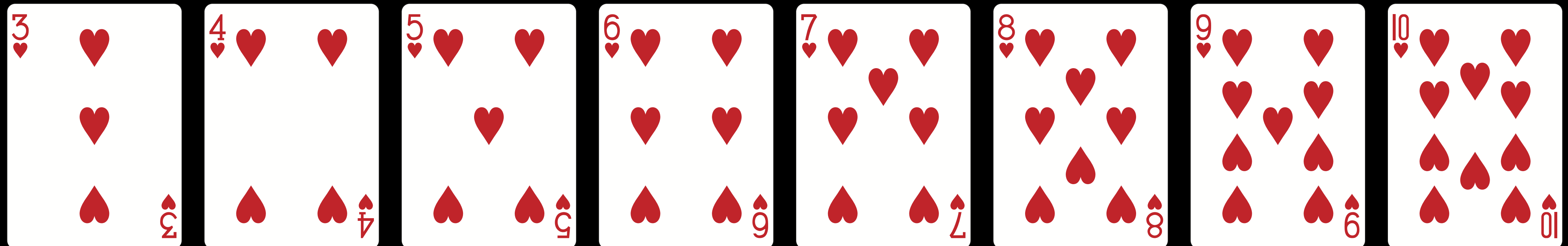
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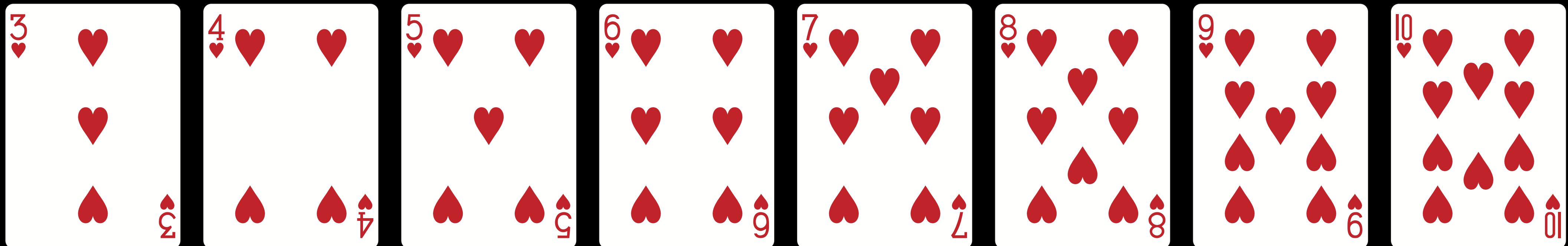
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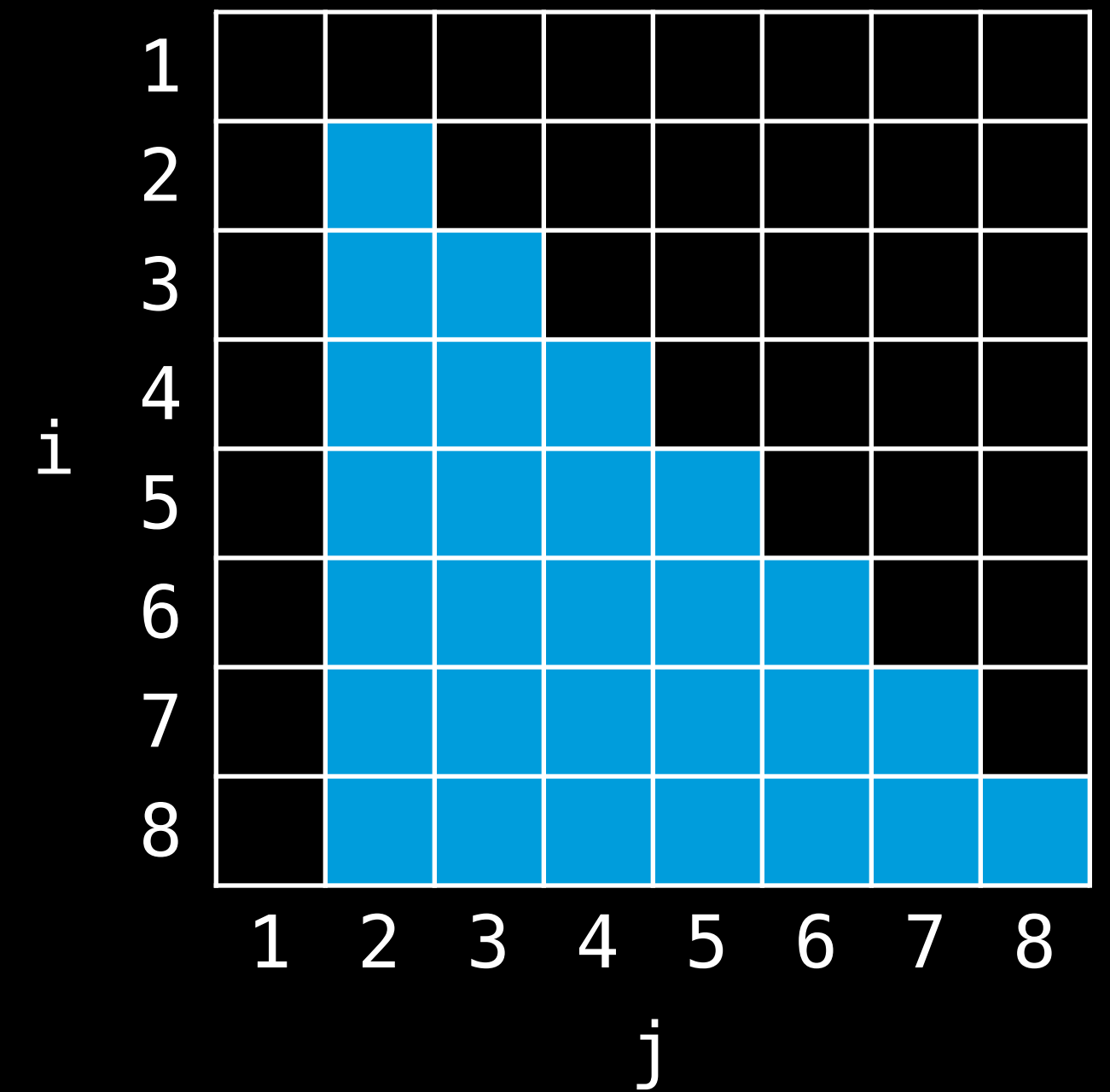
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Sorting

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Sorting

Algorithm sort0(a[], N):

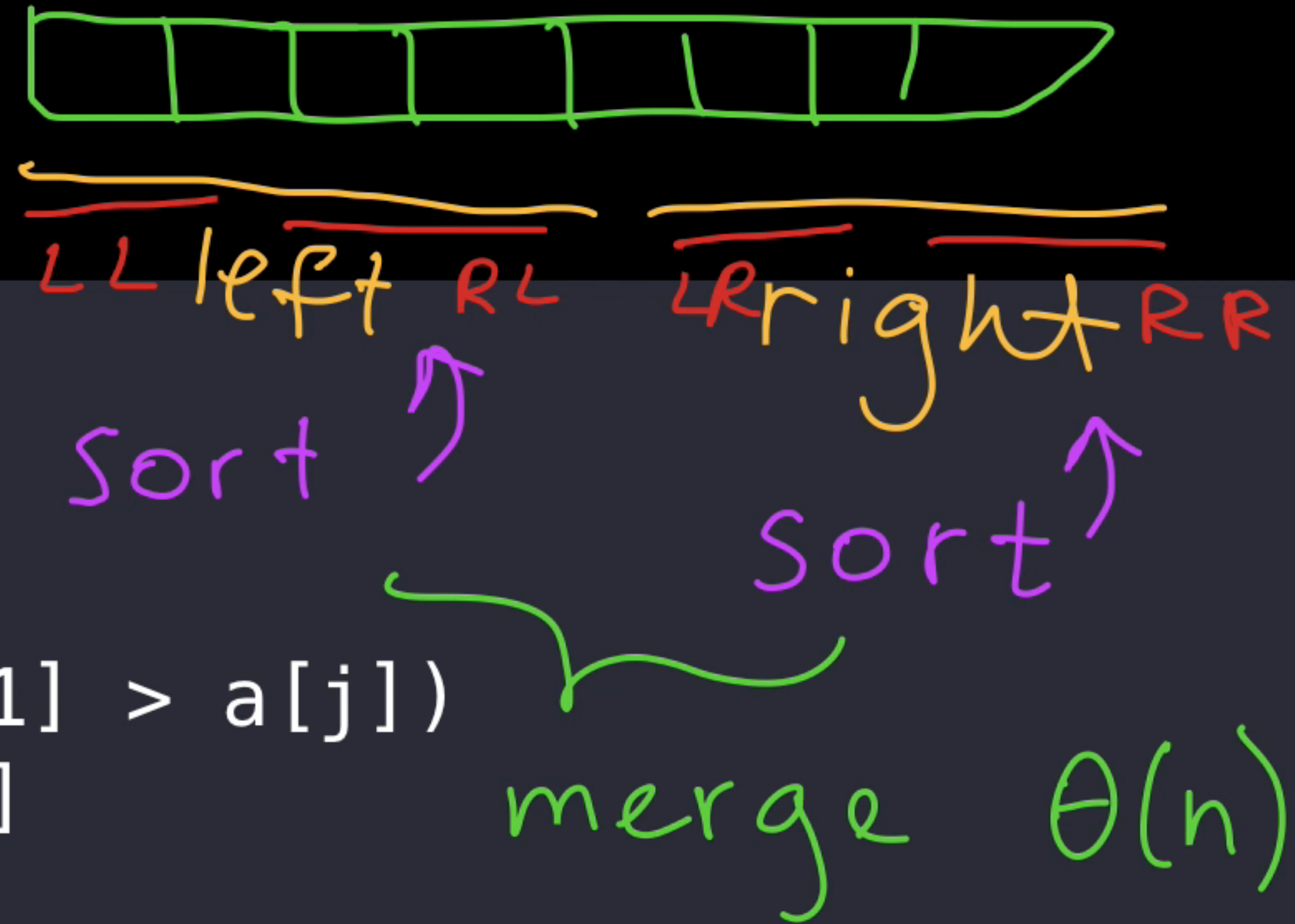
for i=2 to N

 j=i

while (j > 1) and (a[j - 1] > a[j])

swap a[j] and a[j - 1]

 --j



$$T(n) = 2 T\left(\frac{n}{2}\right) + n$$

$$a = 2$$

$$b = 2$$

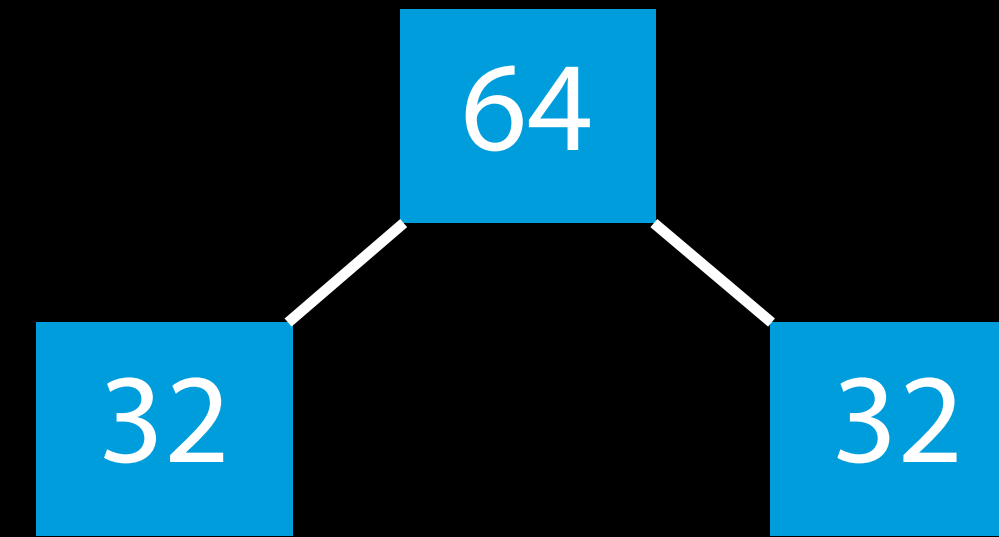
$$c = 1$$

Merge sort: $\Theta(n \log n)$

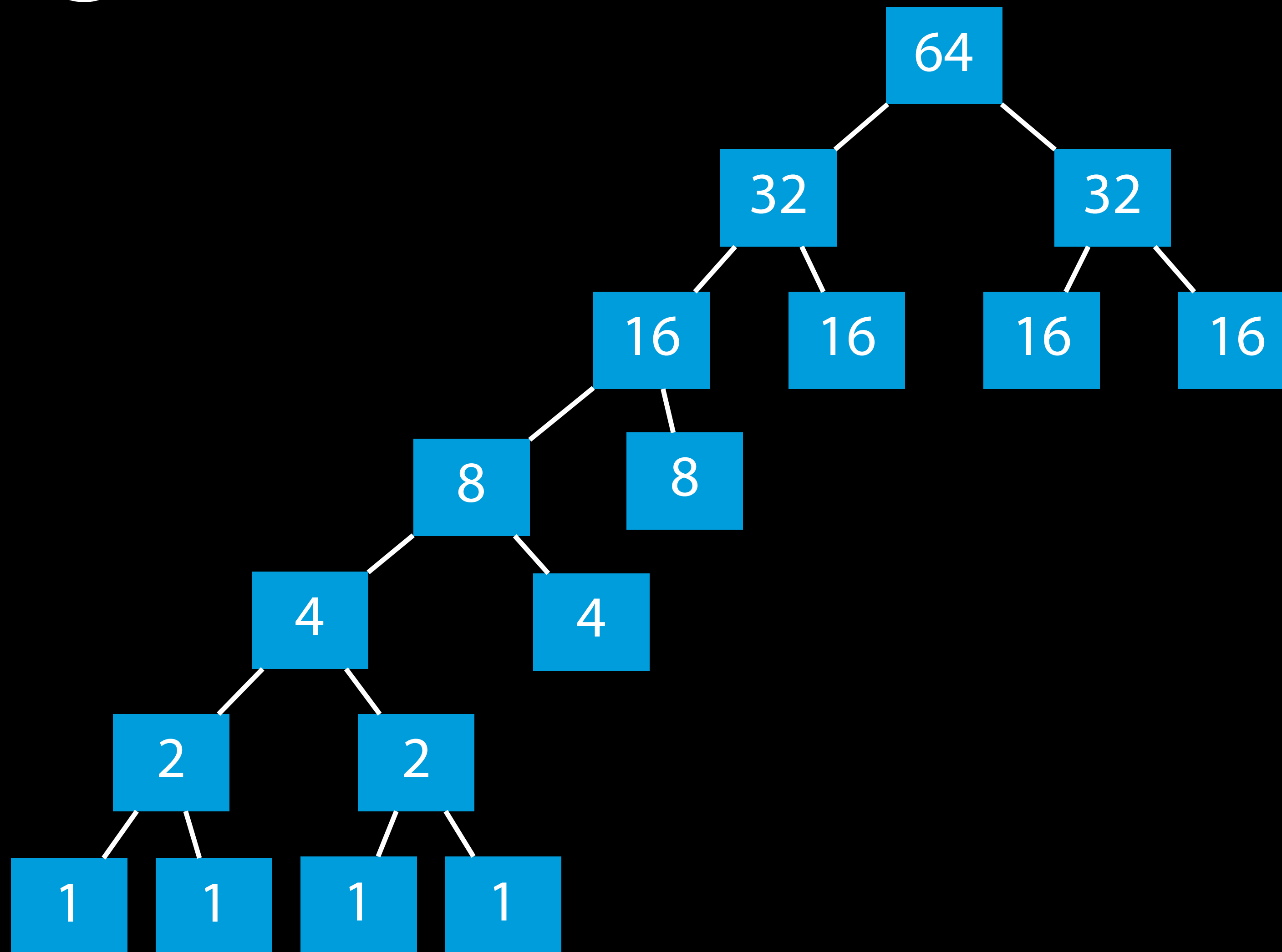
$$2 = 2^1 \rightarrow \text{case 2}$$

$\log n$ times

Sorting



Sorting



Sort/merge

merge

Implement **merge**, a function that combines the elements of two sorted vectors into a single vector and returns the result.

```
vector<int> merge(const vector<int> &a, const vector<int> &b);
```

For example, if **a** contains {1, 2, 4} and **b** contains {2, 3, 5}, **merge** should return a vector containing {1, 2, 2, 3, 4, 5}.

Templates

Function templates

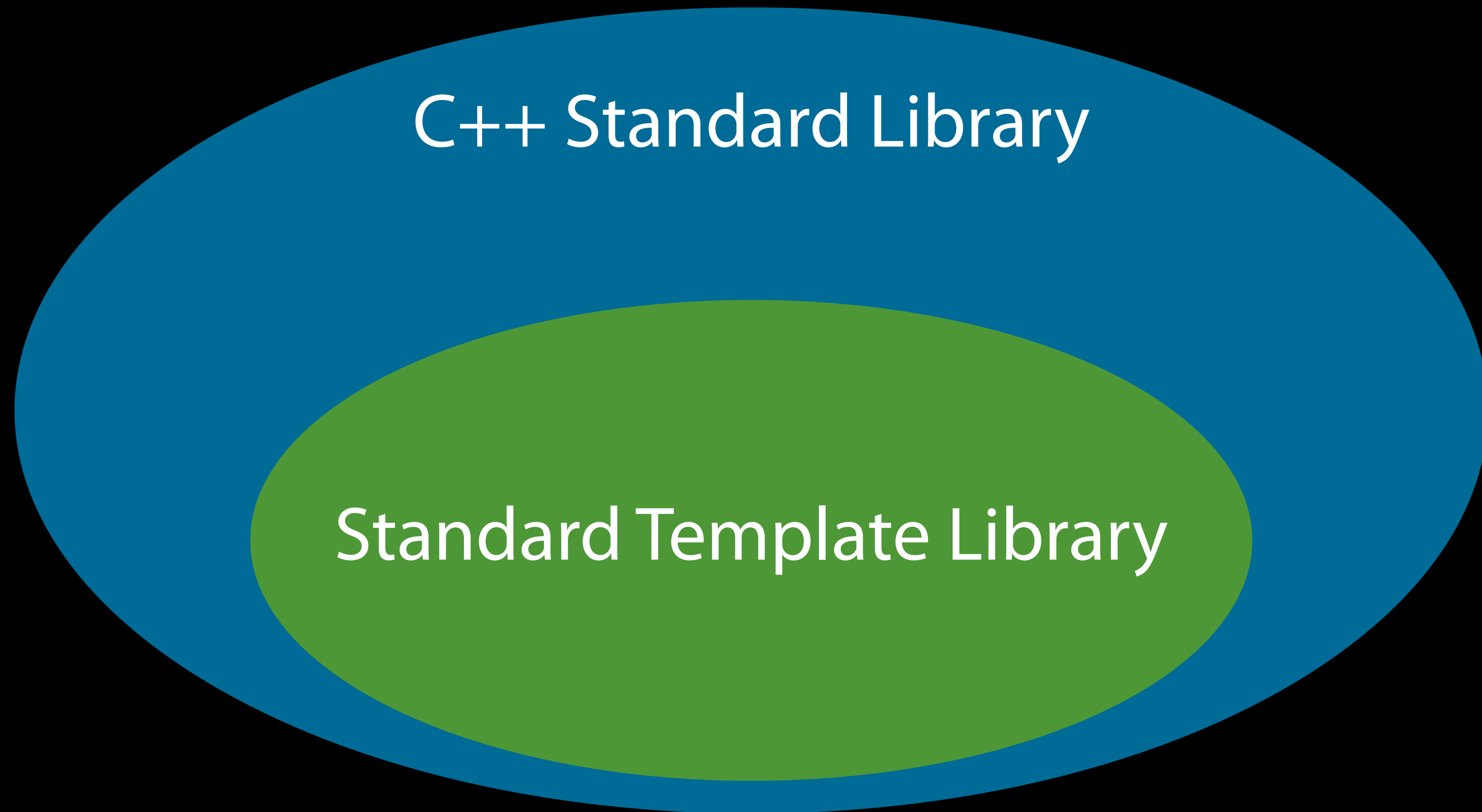
```
template <typename T>  
void swapValues(T& a, T& b) {  
    T temporaryA = a;  
    a = b;  
    b = temporaryA;  
}
```

Class templates

```
template <typename T>
class NamedStack {
    vector<T> items;
    string name;
public:
    NamedStack(string newName): name(newName) {};
    void push(T newItem) {
        items.push_back(newItem);
    }
    // ...
};
```

Standard Template Library

Standard Template Library



Standard Template Library

Algorithms

Containers

Standard Template Library

#: A

Algorithms

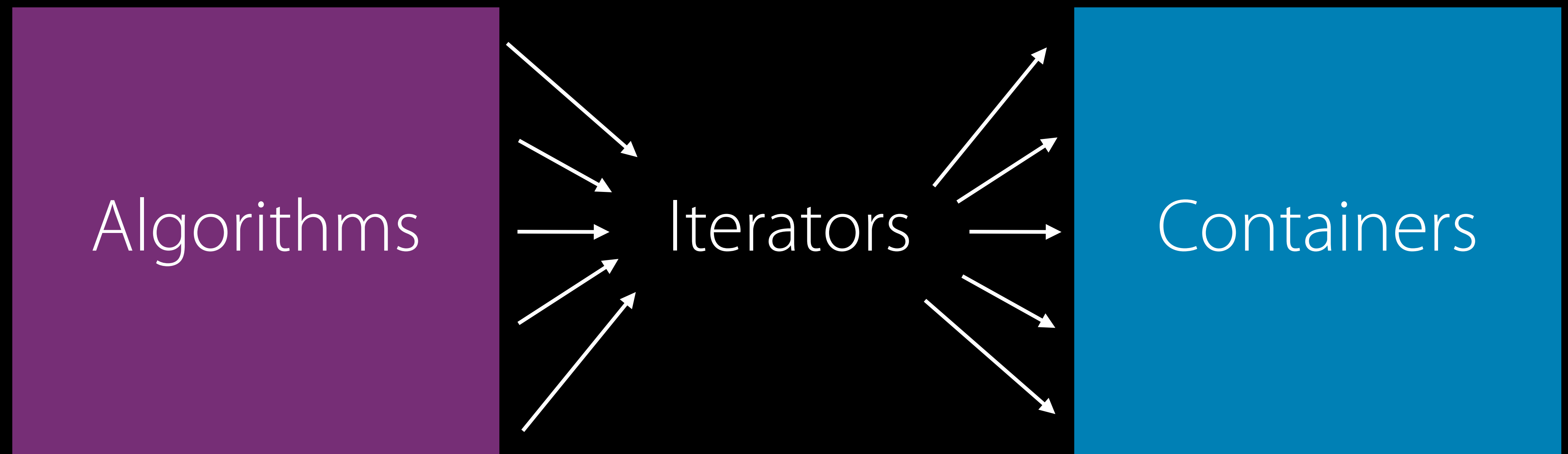
#: C

Containers
classes

member
function

~~Total impl.: $A \times C$~~

Standard Template Library



$A + C$ implementations for A algorithms and C containers.

Reasons to use STL

Code reuse

Efficiency

Less buggy

Standardized, guaranteed availability

Easier to understand others' code

Good knowledge of data structures and algorithms

Iterators

Iterators

Random access iterators: random access

Bidirectional iterators: forward and backward moving

Forward iterators: forward moving

Input iterators: read only, forward moving

Output iterators: write only, forward moving

Iterators

STL containers

Random access iterators: random access

$it + n, it - n$ $< >$

Bidirectional iterators: forward and backward moving

Forward iterators: forward moving

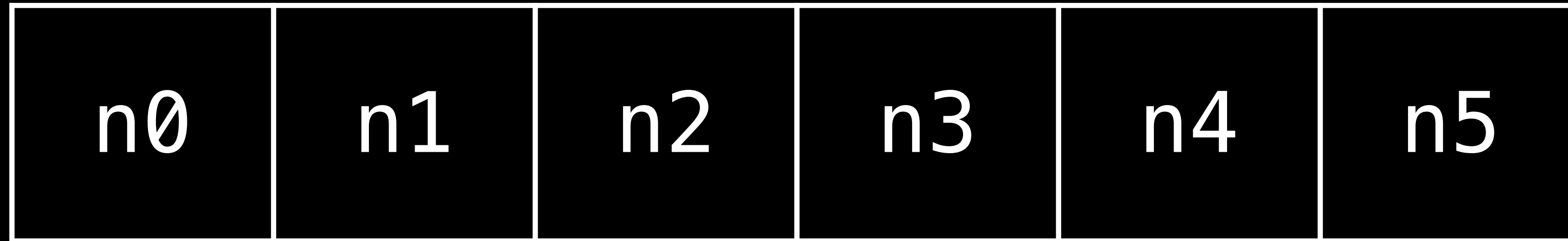
$*$ $++$ $==$ $!=$

Input iterators: read only, forward moving

Output iterators: write only, forward moving

Iterators

`c.begin()`



`c.end()`

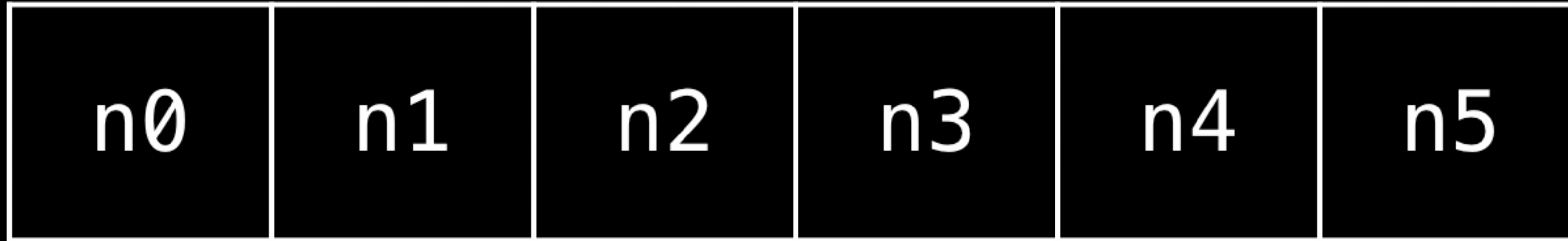


```
// c is some container
for (auto it = c.begin(); it != c.end(); ++it) {
    cout << *it << " ";
}
```

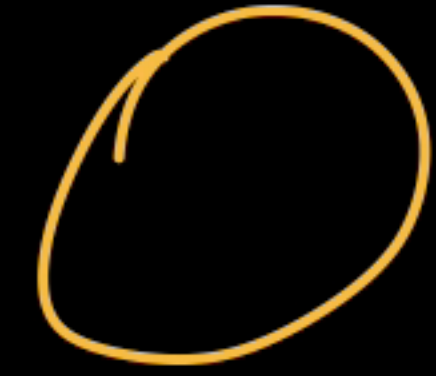
Iterators

$[begin, end)$ ← half-open range

`c.begin()`



`c.end()`



```
// c is some container
for (auto it = c.begin(); it != c.end(); ++it) {
    cout << *it << " ";
}
```

Iterators

Pure abstraction!

Every container has an `iterator` and a `const_iterator`

Iterators

Pure abstraction!

Every container has an iterator and a const_iterator

```
vector<int>::iterator it = v.begin()
```

```
vector<int>::const_iterator cit = v.cbegin()
```

Iterator functions

```
advance(it, 5);
```

```
distance(it1, it2);
```

Iterator adapters

Insert iterators

Stream iterators

Reverse iterators

Move iterators

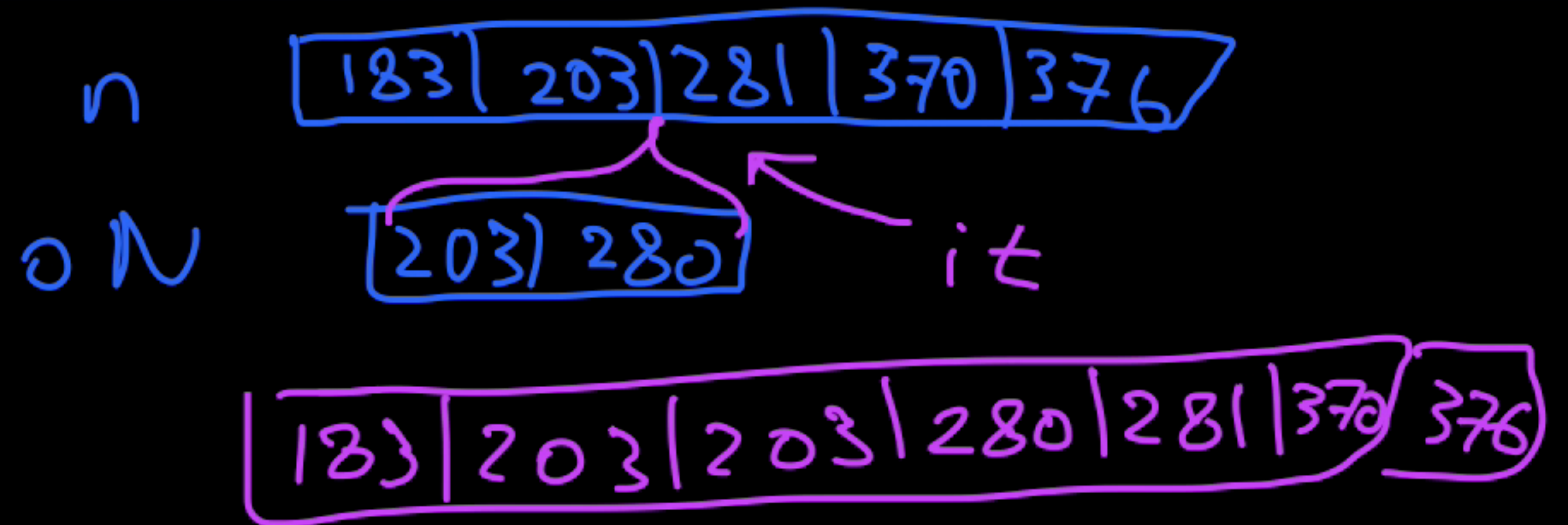
Insert iterators

```
vector<int> numbers = {183, 203, 281, 370, 376};  
vector<int> otherNumbers = {203, 280};  
vector<int>::iterator it = find(numbers.begin(),  
                                numbers.begin(), 281);  
insert_iterator<vector<int>> insertIt(numbers, it);  
copy(numbers.begin(), numbers.end(), insertIt);
```

Insert iterators

#include <algorithm>

```
vector<int> numbers = {183, 203, 281, 370, 376};  
vector<int> otherNumbers = {203, 280};  
vector<int>::iterator it = find(numbers.begin(),  
                                numbers.beginend(), 281);  
insert_iterator<vector<int>> insertIt(numbers, it);  
copy(numbers.begin(), numbers.end(), insertIt);
```



Stream iterators

```
vector<int> inputNumbers;  
copy(istream_iterator<int>(cin),  
      istream_iterator<int>(),  
      back_inserter(inputNumbers));  
  
copy(istream_iterator<int>(cin),  
      istream_iterator<int>(),  
      ostream_iterator<int>(cout, "\n"));
```

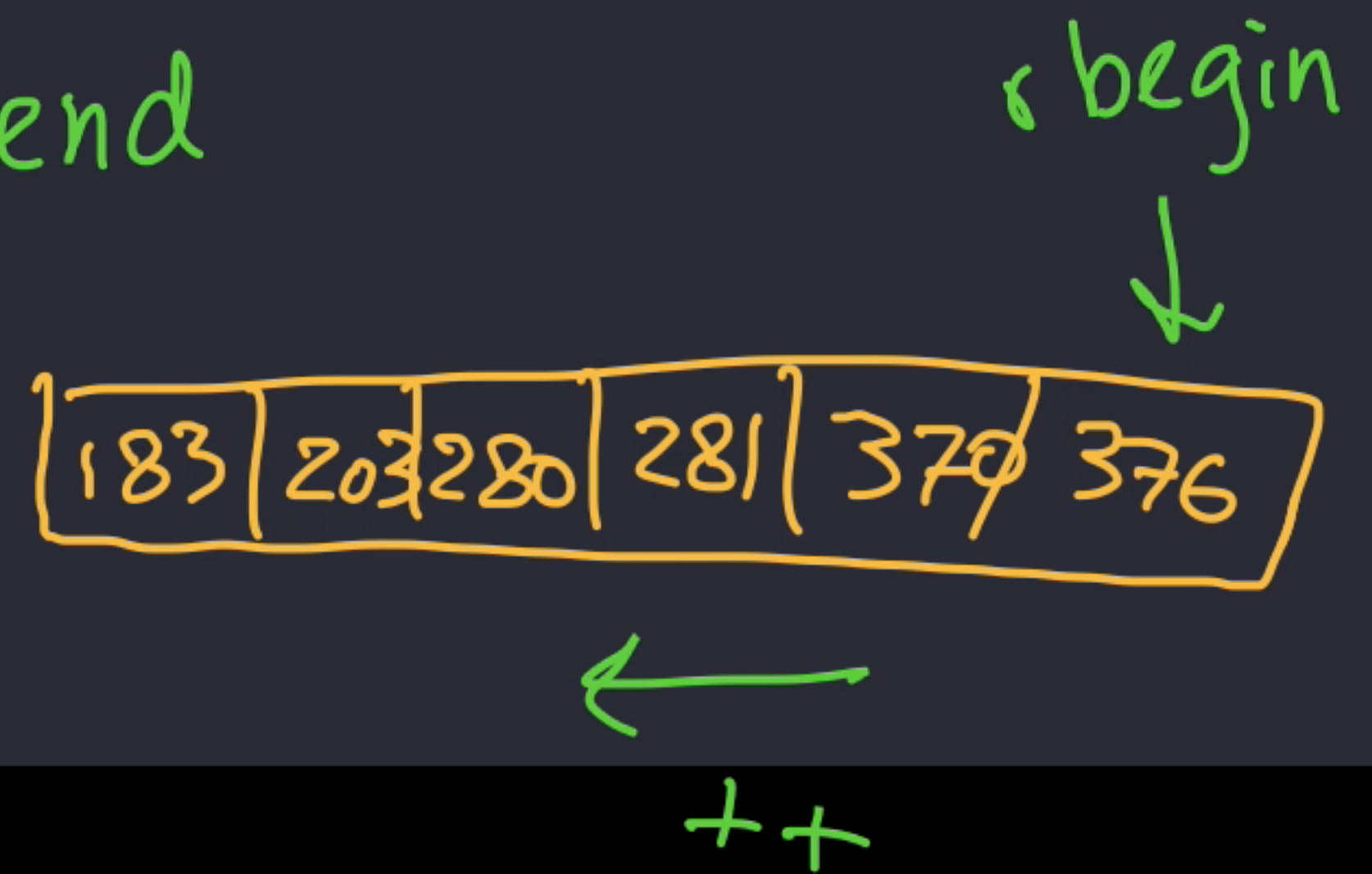
Reverse iterators

```
vector<int> numbers = {183, 203, 280, 281, 370, 376};  
reverse_iterator<vector<int>::iterator> reverseIt;  
  
for (reverseIt = numbers.rbegin();  
     reverseIt != numbers.rend();  
     ++reverseIt) {  
    cout << *reverseIt << endl;  
}
```

Reverse iterators

```
vector<int> numbers = {183, 203, 280, 281, 370, 376};  
reverse_iterator<vector<int>::iterator> reverseIt;
```

```
for (reverseIt = numbers.rbegin();  
     reverseIt != numbers.rend();  
     ++reverseIt) {  
    cout << *reverseIt << endl;  
}
```



Containers

Containers

Sequence containers:

vector, deque, list, forward list, array

Associative containers:

(multi)set, (multi)map

Unordered associative containers:

unordered_(multi)set, unordered_(multi)map

Container adapters:

queue, stack, priority queue

Containers

Sequence containers:

vector, deque, list, forward list, array, string

random access it

Associative containers: bidir it forward it

(multi)set, (multi)map

Unordered associative containers:

unordered_(multi)set, unordered_(multi)map

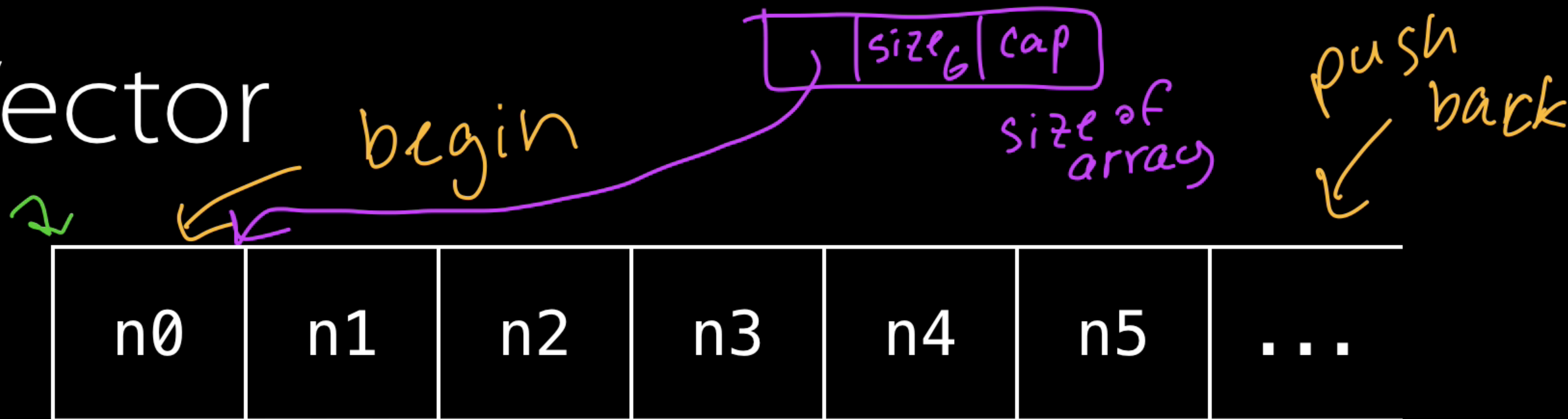
Container adapters:

queue, stack, priority queue

Vector

n_0	n_1	n_2	n_3	n_4	n_5	$\dots$
-------	-------	-------	-------	-------	-------	---------

Vector



contiguous block of memory

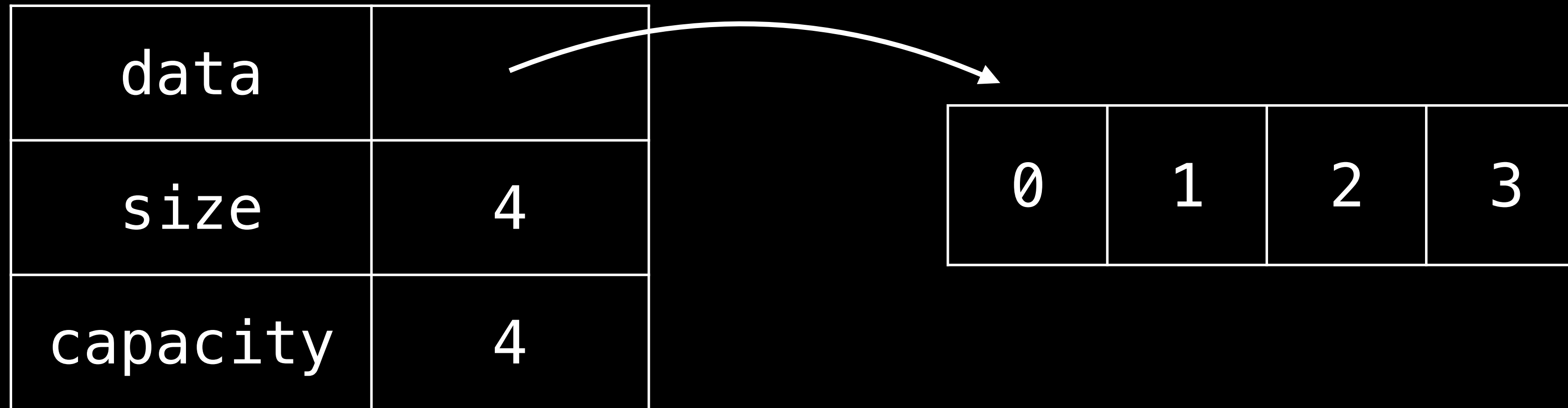
insert / remove
beginning $O(n)$ middle $O(n)$ end $O(1)$

`int * arr = &v[0];`
`* (arr + 1);`
search: $O(n)$

resize
reserve
size
capacity

```
vector::push_back()
```

vector::push_back()



vector::push_back()

data	
size	5
capacity	8



vector::push_back()

data	
size	5
capacity	8



capacity $\times 2$



vector::push_back()

data	
size	6
capacity	8



vector::push_back()

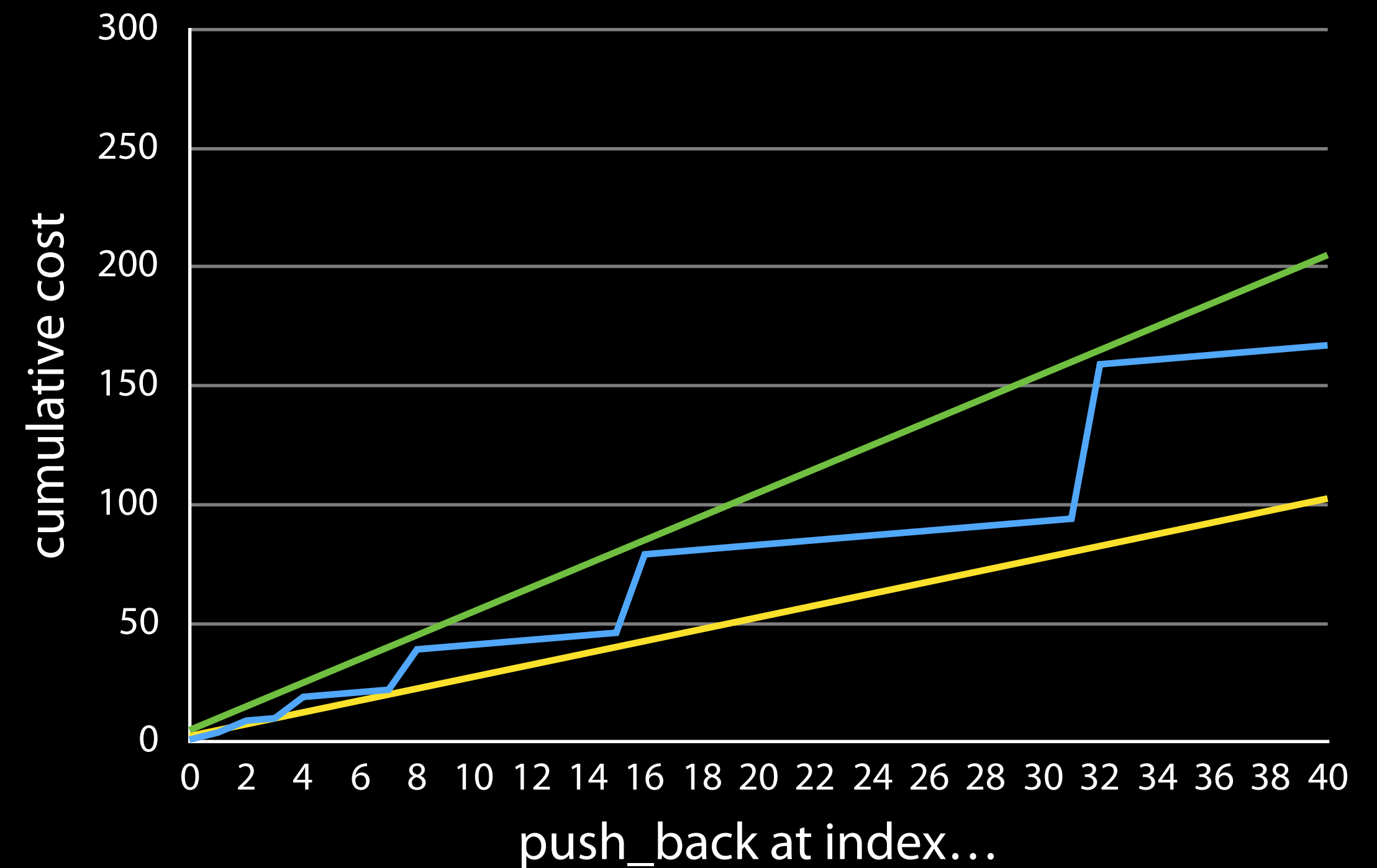
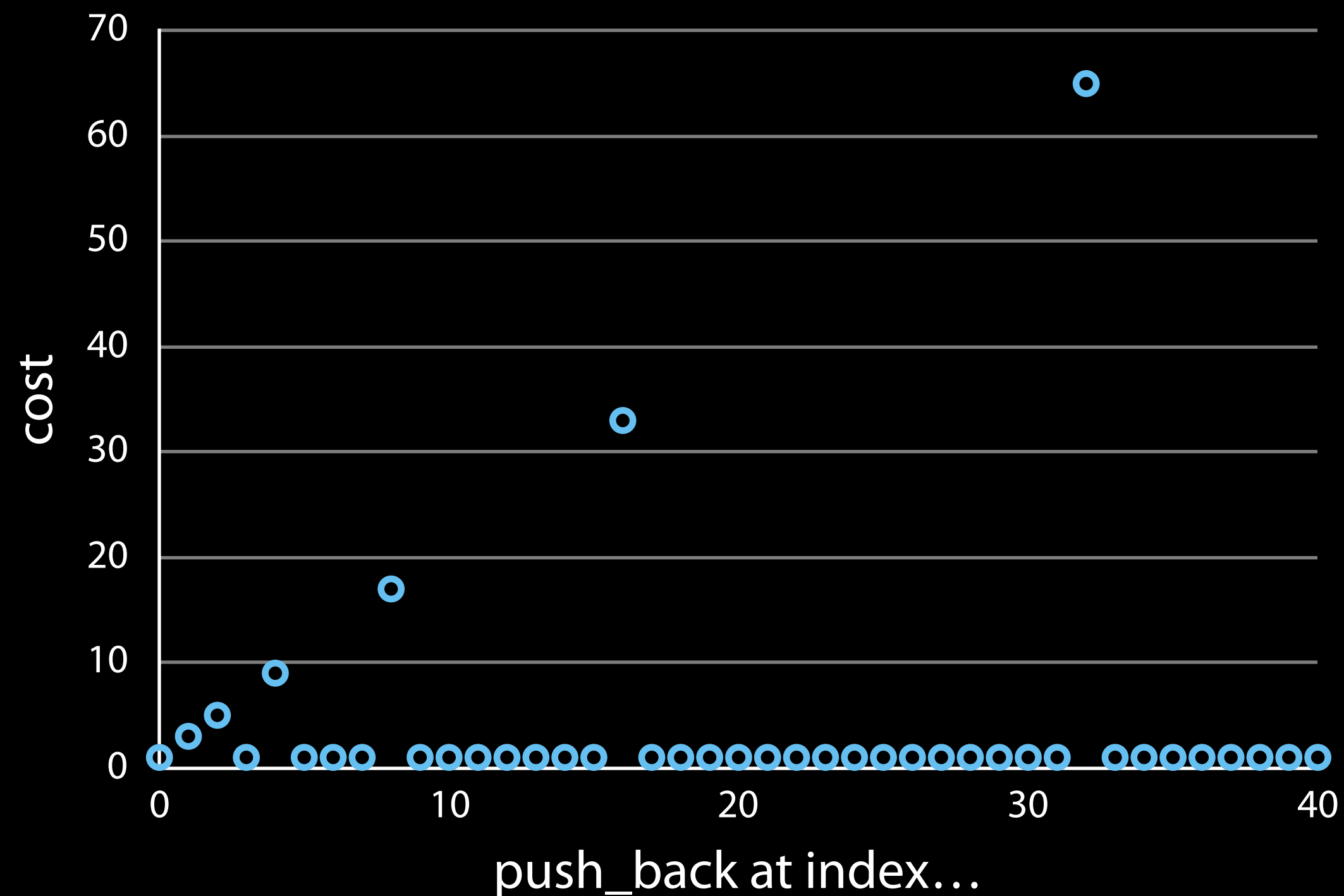
push_back at i...	0	1	2	3	4	5	6	7	8
size									
capacity									
write cost									
resize cost									
total cost									
cumulative cost									
average cost									

vector::push_back()

push_back at i...	0	1	2	3	4	5	6	7	8
size	1	2	3	4	5	6	7	8	9
capacity	1	2	4	4	8	8	8	8	16
write cost	1	1	1	1	1	1	1	1	1
resize cost	0	2	4	0	8	0	0	0	16
total cost	1	3	5	1	9	1	1	1	17
cumulative cost	1	4	9	10	19	20	21	22	39
average cost	1.00	2.00	3.00	2.50	3.80	3.33	3.00	2.75	4.33

Amortized complexity

Average the time required to perform a sequence of operations over all the operations performed.



Iterator invalidation

vector

iterators, pointers and references are invalidated after insertion if new container size is greater than the previous capacity.

deque

iterators, pointers and references are invalidated after insertion (unless inserting at the front/end, then references are unaffected).

list

iterators, pointers and references are unaffected.

Algorithms

```
#include <algorithm>
```

Algorithms

(Mostly loops)

`min_element`

`sort`

`reverse`

`copy`

`find_if`

`for_each`

...

Anagrams

Implement **areAnagrams**, a function that checks if s1 and s2 are anagrams of each other.

```
bool areAnagrams(const string& s1, const string& s2);
```